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# NUMERICAL ANALYSIS OF RESIDUAL STRESSES IN PARTS PRODUCED BY SELECTIVE LASER MELTING PROCESS

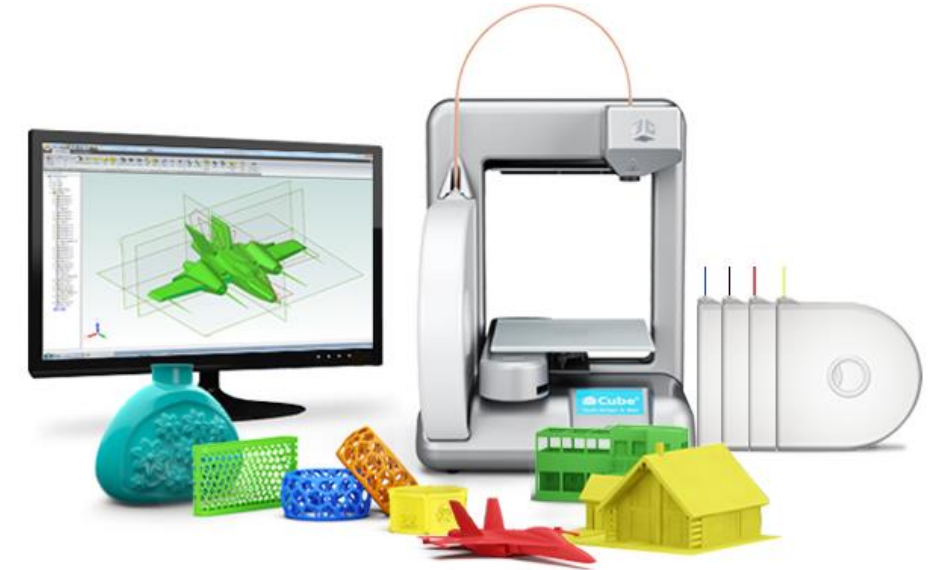
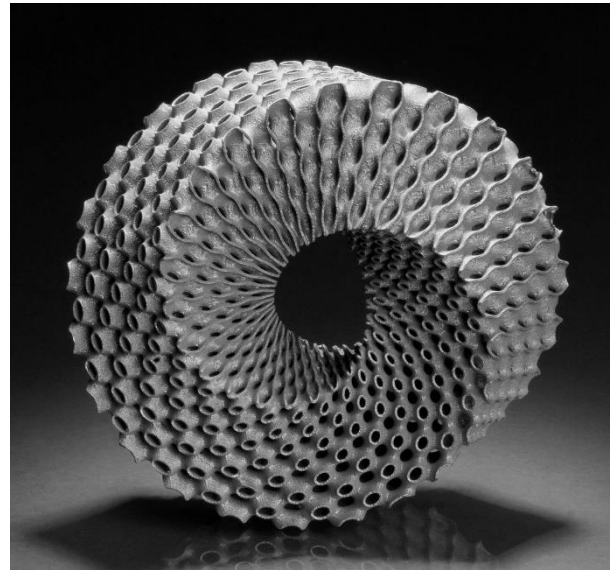
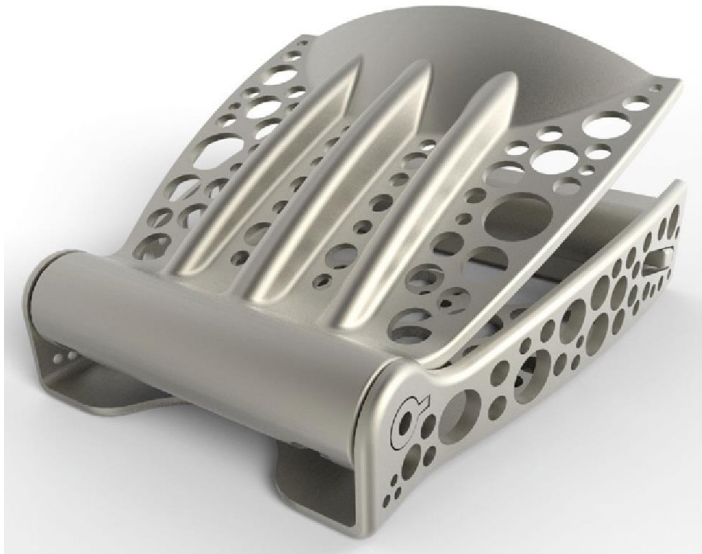
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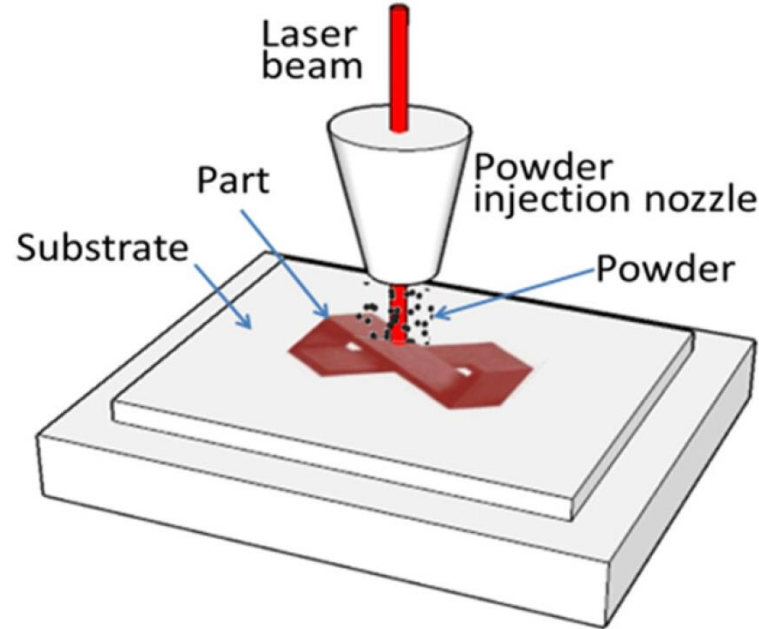
## Additive Manufacturing

- Main **advantages** of the additive manufacturing processes:
  - ✓ Complex part geometry
  - ✓ Variety of products and materials
  - ✓ No time gap between design and prototyping

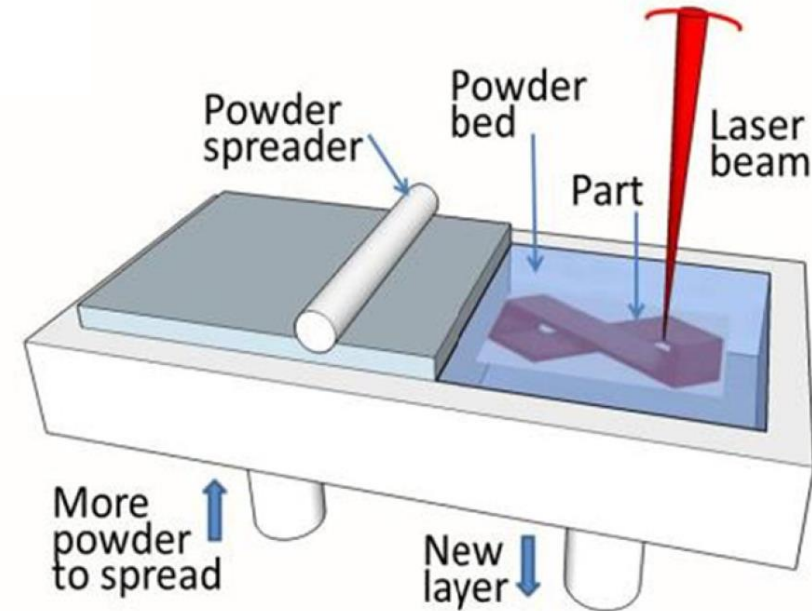


## Powder-based Additive Manufacturing

- **Direct Energy Deposition:** coaxial nozzle to deliver powder to the focal point of a laser
- **Selective Laser Melting:** uses a roller to spread a thin layer of powder before melting the layer



**Direct Energy Deposition (DED)**



**Selective Laser Melting (SLM)**

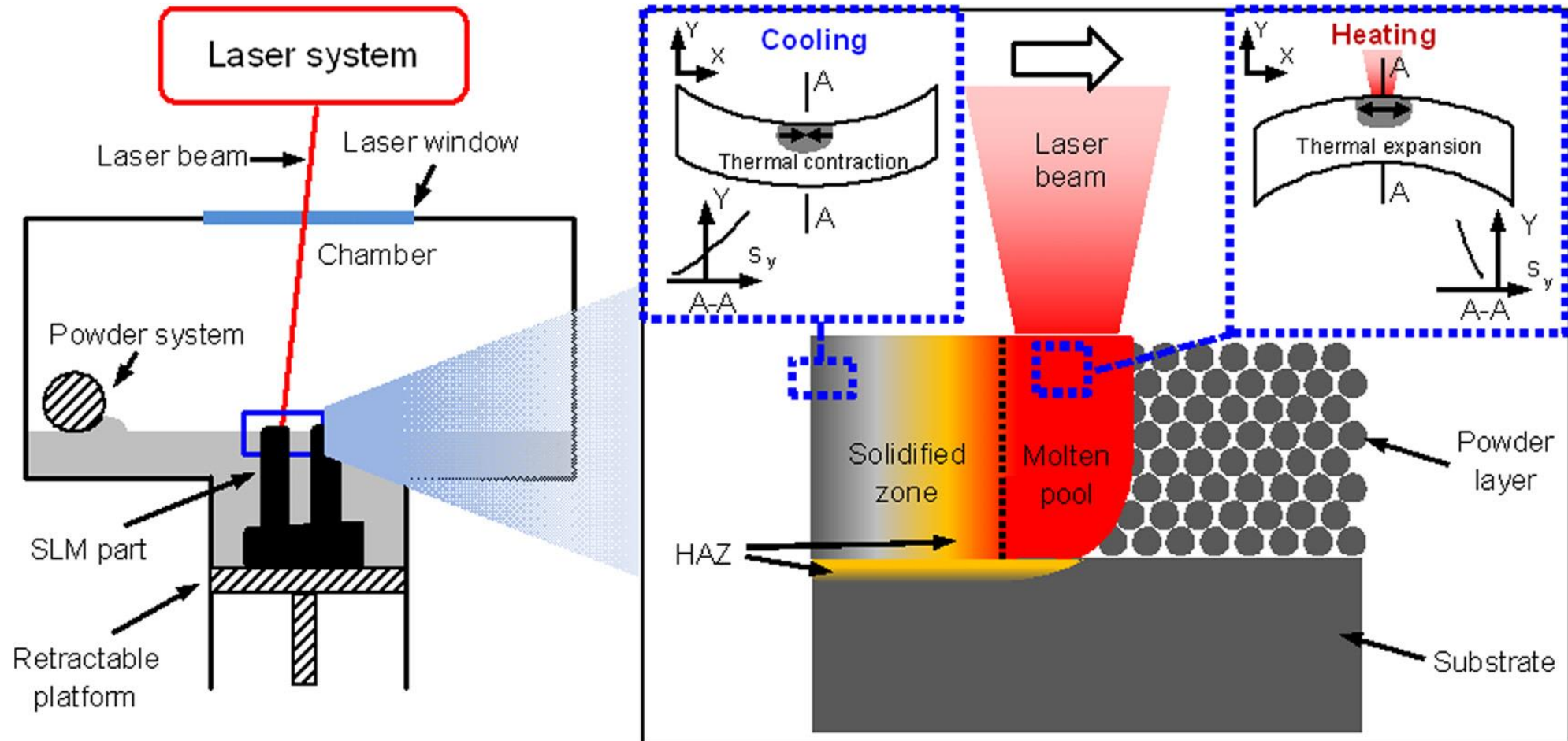
## Selective Laser Melting

- Example of **SLM machine** running



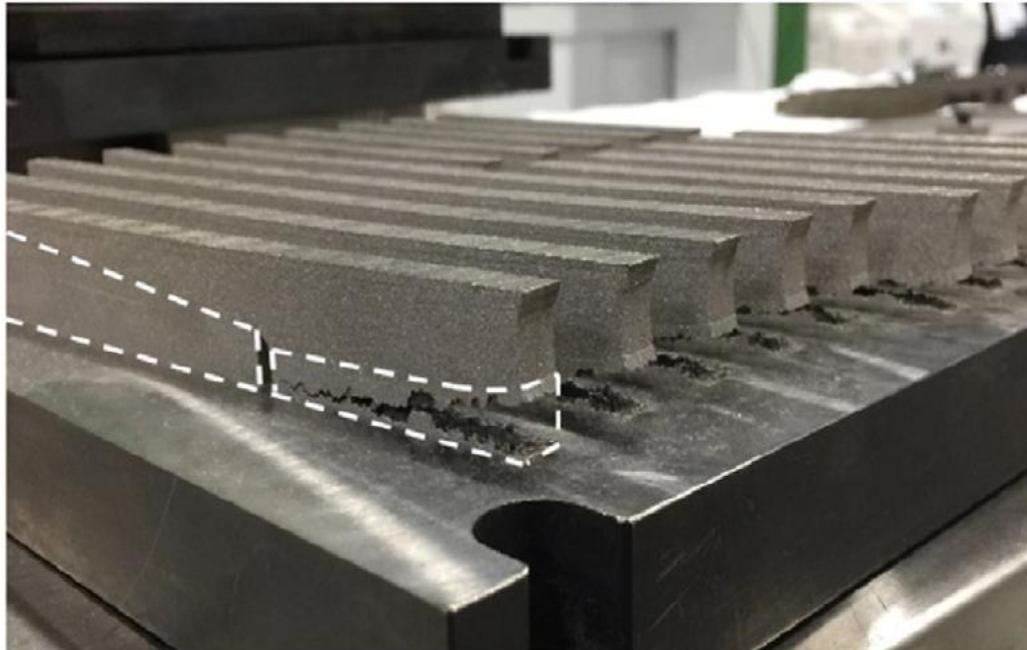
## Selective Laser Melting

- Material phase transformation **from powder to liquid**, which then **cools down to solidification**

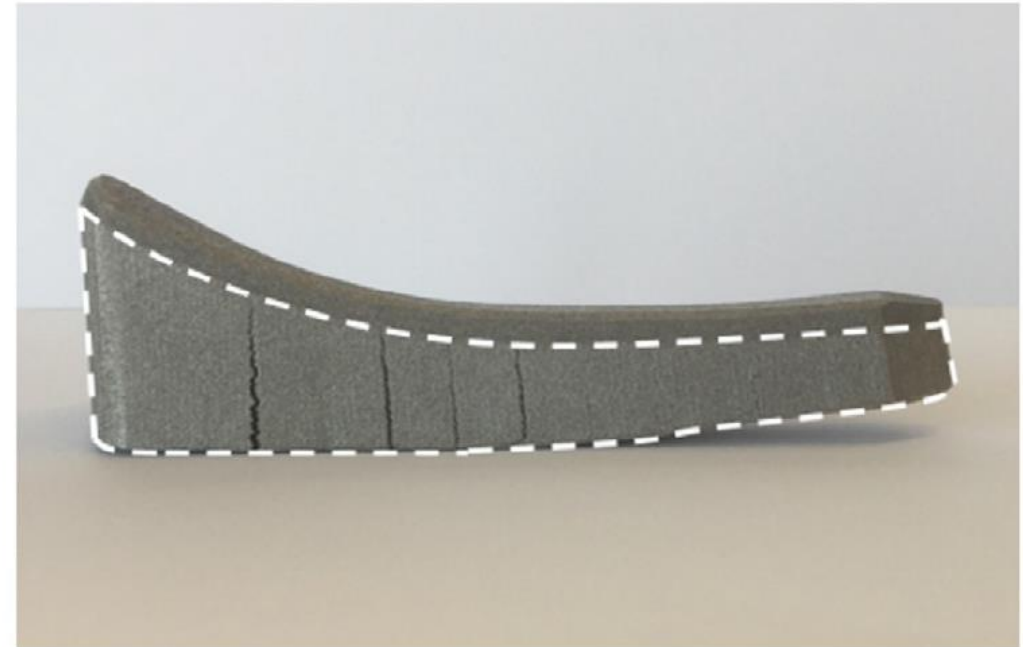


## Selective Laser Melting

- The main drawback is the **high level of residual thermal stresses and large deformation** generated by temperature gradients in a layer-by-layer melting process



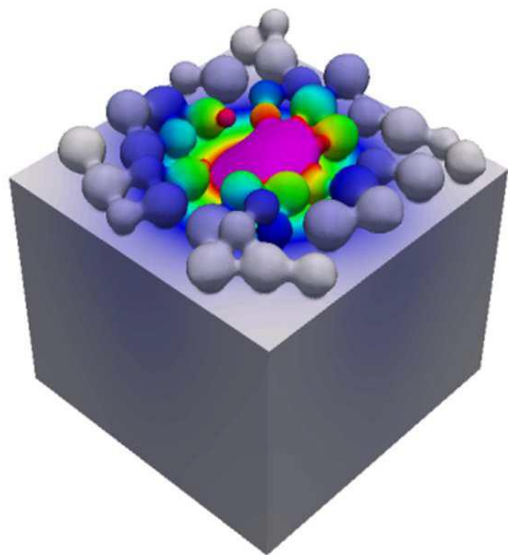
Cracks due to residual stress during the manufacturing



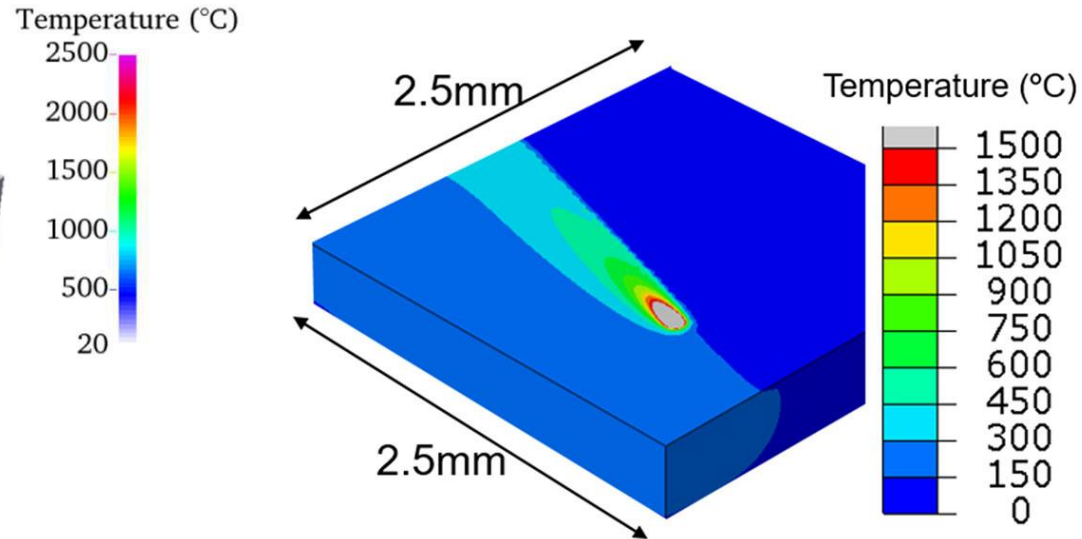
Component deformed after removal from the building chamber

## SLM modelling at different length- and time-scales

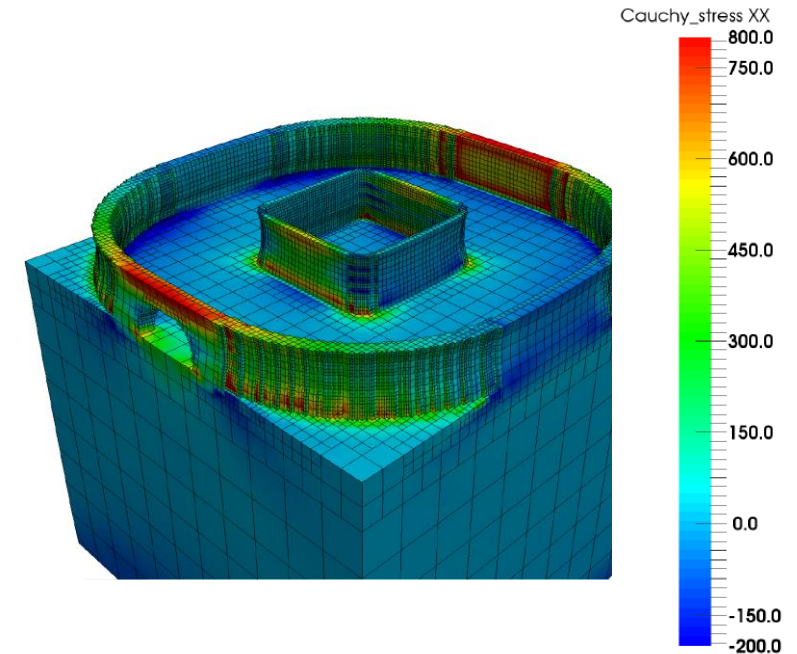
- ❑ **Micro-scale:** modelling the interactions between the laser and particles
- ❑ **Meso-scale:** modelling sub-regions of the process, typically a number of scan vectors
- ❑ **Macro-scale:** modelling information for large regions or parts



Micro-scale



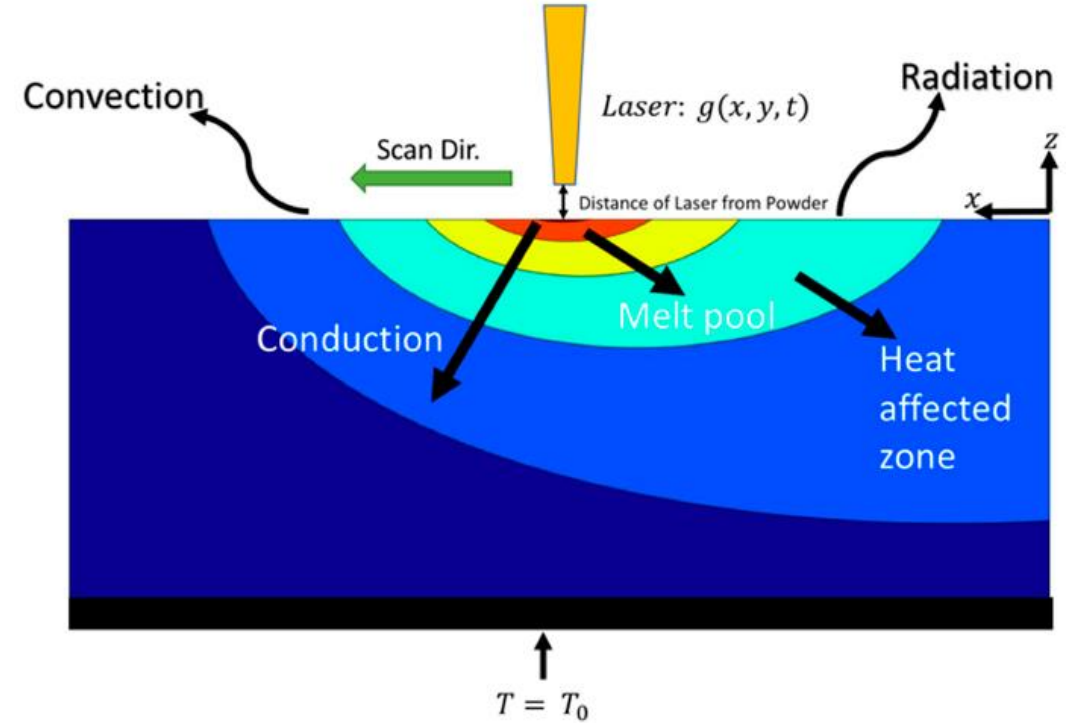
Meso-scale



Macro-scale

## Heat transfer modeling

- **Heat conduction** within the solid/powder
- **Heat generated** by the laser beam
- **Heat losses** by convection/radiation
- **Transient heat conduction** within a solid material



$$k \left( \frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right) + \dot{q} = \rho c_p \frac{\partial T}{\partial t}$$

Thermal conductivity  $k$ , Power generation per unit volume  $\dot{q}$ , Mass density  $\rho$ , Specific heat  $c_p$ , Temperature  $T$ , Time  $t$ .

Temperature dependent material properties are required



## Heat transfer modeling

- Laser heat input modelled by a **volumetric Gaussian heat source**

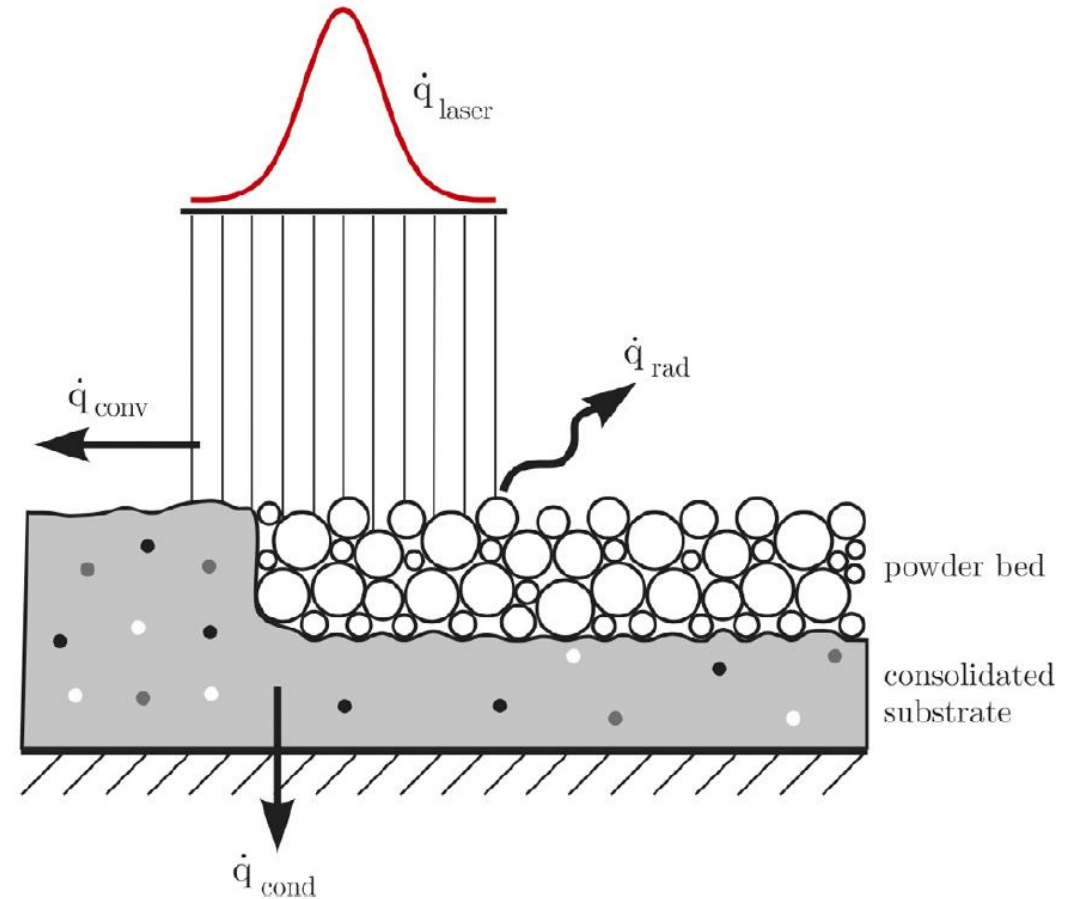
$$\dot{q} = \frac{2^{5/2} \beta P}{\pi^{3/2} r_0^3} \exp \left\{ -2 \frac{x^2 + y^2 + z^2}{r_0^2} \right\}$$

Laser spot size

- Heat loss by **natural convection** between the exposed powder bed surface and the environment

$$\dot{q}_c = h_c (T - T_\infty)$$

Heat convection coefficient      Environment temperature



## Mechanical modeling

- Balance of linear momentum under quasi-static analysis:

$$\text{div}(\boldsymbol{\sigma}) + \mathbf{b} = \mathbf{0}$$

Body forces  
Stress tensor

- Total strain increment:

$$\Delta \boldsymbol{\varepsilon}^{\text{total}} = \Delta \boldsymbol{\varepsilon}^{\text{e}} + \Delta \boldsymbol{\varepsilon}^{\text{p}} + \Delta \boldsymbol{\varepsilon}^{\text{th}}$$

Elastic strain increment      Plastic strain increment      Thermal strain increment

- Elastic strain:**

$$\boldsymbol{\sigma}^{\text{e}} = \mathbf{C} : \boldsymbol{\varepsilon}^{\text{e}}$$

Elastic moduli

- Plastic strain increment:**

$$\Delta \boldsymbol{\varepsilon}^{\text{p}} = \lambda \frac{\partial f}{\partial \boldsymbol{\sigma}}$$

Associated flow rule

$$f = \sigma_{\text{vM}} - \sigma_y \leq 0$$

von Mises yield criteria

$$\sigma_y = K(\varepsilon_0 + \bar{\varepsilon}^{\text{p}})^n$$

Swift law

- Thermal strain:**

$$\boldsymbol{\varepsilon}^{\text{th}} = (\alpha_T (T - T_{\text{ref}}) - \alpha_{\text{ini}} (T_{\text{ini}} - T_{\text{ref}})) \mathbf{I}$$

Volumetric thermal expansion coefficients

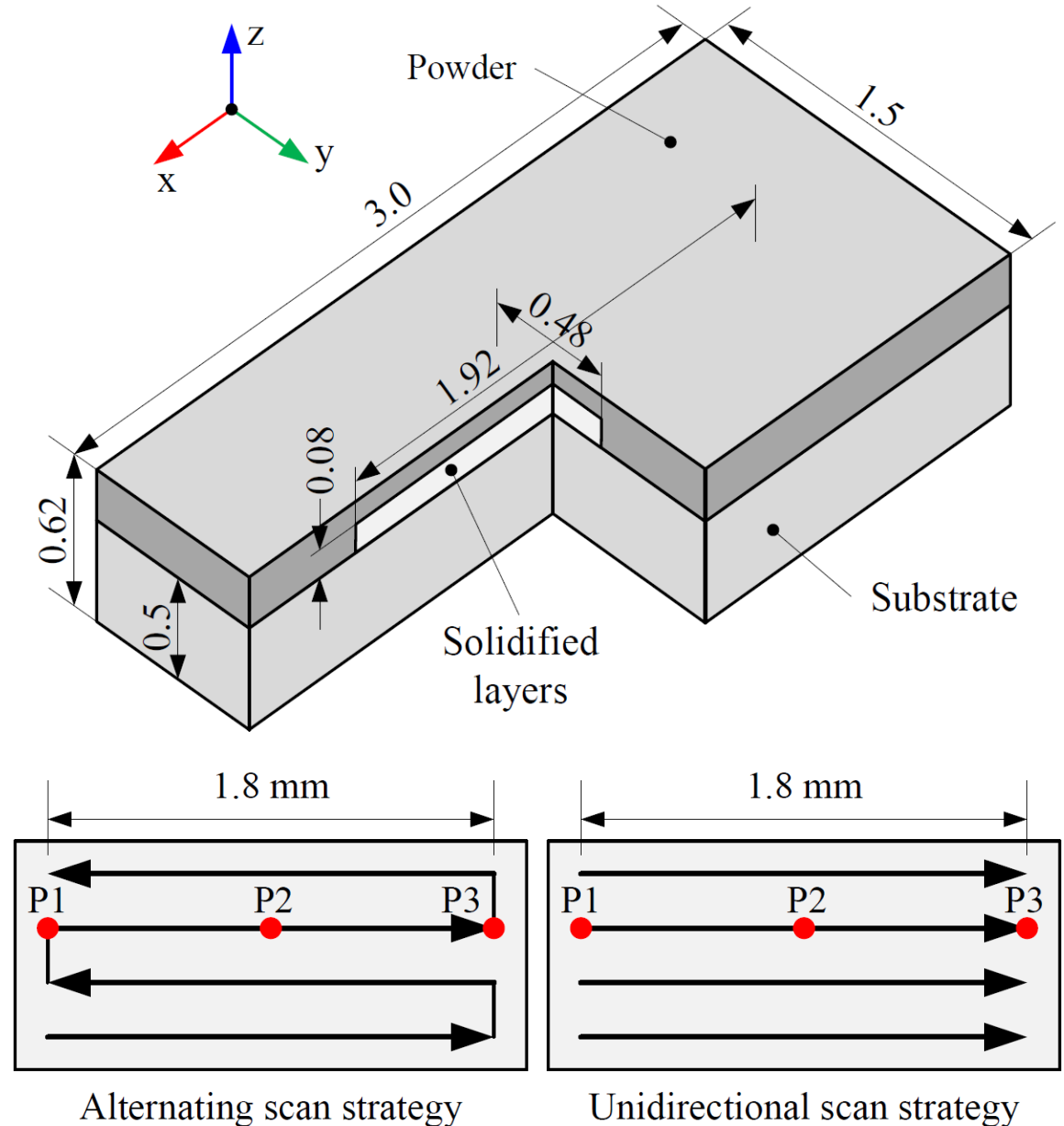
## Numerical algorithms

- In-house finite element code **DD3IMP**, originally developed for sheet metal forming simulation
- Thermo-mechanical coupling using a **staggered algorithm**
- **Euler's backward time integration** for the transient heat conduction problem
- Finite deformation is described by an **updated Lagrangian scheme**
- **Fully implicit Newton–Raphson scheme** for the mechanical solution
- Thermal and mechanical solutions using the **same finite element mesh** (8-node hexahedral elements)

## SLM process conditions

- **Multi-track** in a **single powder layer** deposition, scanned over solidified layers
- Material of powder and substrate: **Ti-6Al-4V**
- Finite element mesh with 10  $\mu\text{m}$  of edge size
- 2 different **scanning strategies**

Process parameter	Value
Laser power [W]	83
Laser absorptivity	0.35
Laser spot radius [ $\mu\text{m}$ ]	50
Scanning speed [mm/s]	600
Layer thickness [ $\mu\text{m}$ ]	40
Hatching distance [ $\mu\text{m}$ ]	120
Preheating temperature [ $^{\circ}\text{C}$ ]	200



## Thermo-physical material properties

- **Liquid with constant thermo-mechanical properties.** The thermal conductivity coefficient was artificially increased to account for the convective heat transfer within the melt pool
- Weak mechanical strength of the powder and liquid

Powder, solid and liquid  
Ti-6Al-4V

Property	Powder	Solid	Liquid
$\rho$ [kg/m <sup>3</sup> ]	2600	4300	4300
$c_p$ [J/kg·K]	-	-	820
$k$ [W/m·K]	-	-	42
$\alpha$ [ $\times 10^{-6}$ 1/K]	1.2	12.0	0.0
$E$ [GPa]	0.05	-	0.05
$\nu$ [-]	0.34	0.34	0.34
$\sigma_0$ [MPa]	1.5	-	1.5
$K$ [MPa]	10	-	10
$n$ [-]	0.35	0.35	0.35

Powder Ti-6Al-4V

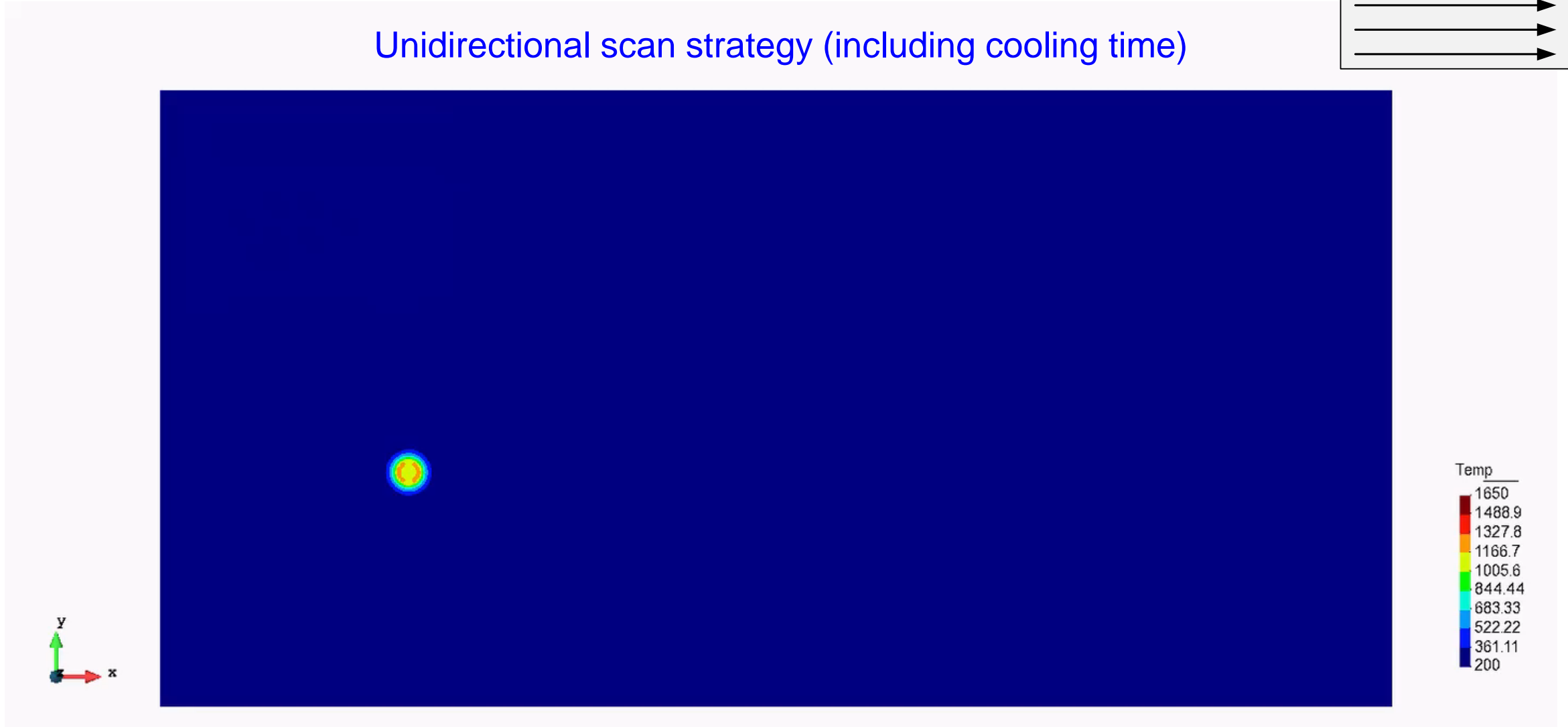
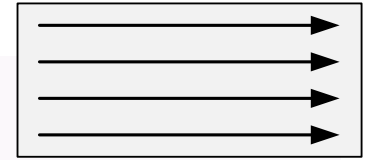
$T$ [°C]	$c_p$ [J/kg·K]	$k$ [W/m·K]
200	505	0.104
500	473	0.078
800	507	0.279
1000	610	0.813
1300	951	1.27
1650	1000	1.80

Solid Ti-6Al-4V

$T$ [°C]	$c_p$ [J/kg·K]	$k$ [W/m·K]	$E$ [GPa]	$\sigma_0$ [MPa]	$K$ [MPa]
200	566	9.3	100	630	1500
650	646	15.3	55	300	770
761	665	17.0	20	110	350
872	685	18.5	10	55	120
1094	760	24.0	3	17	60
1650	820	27.0	0.05	1.5	10

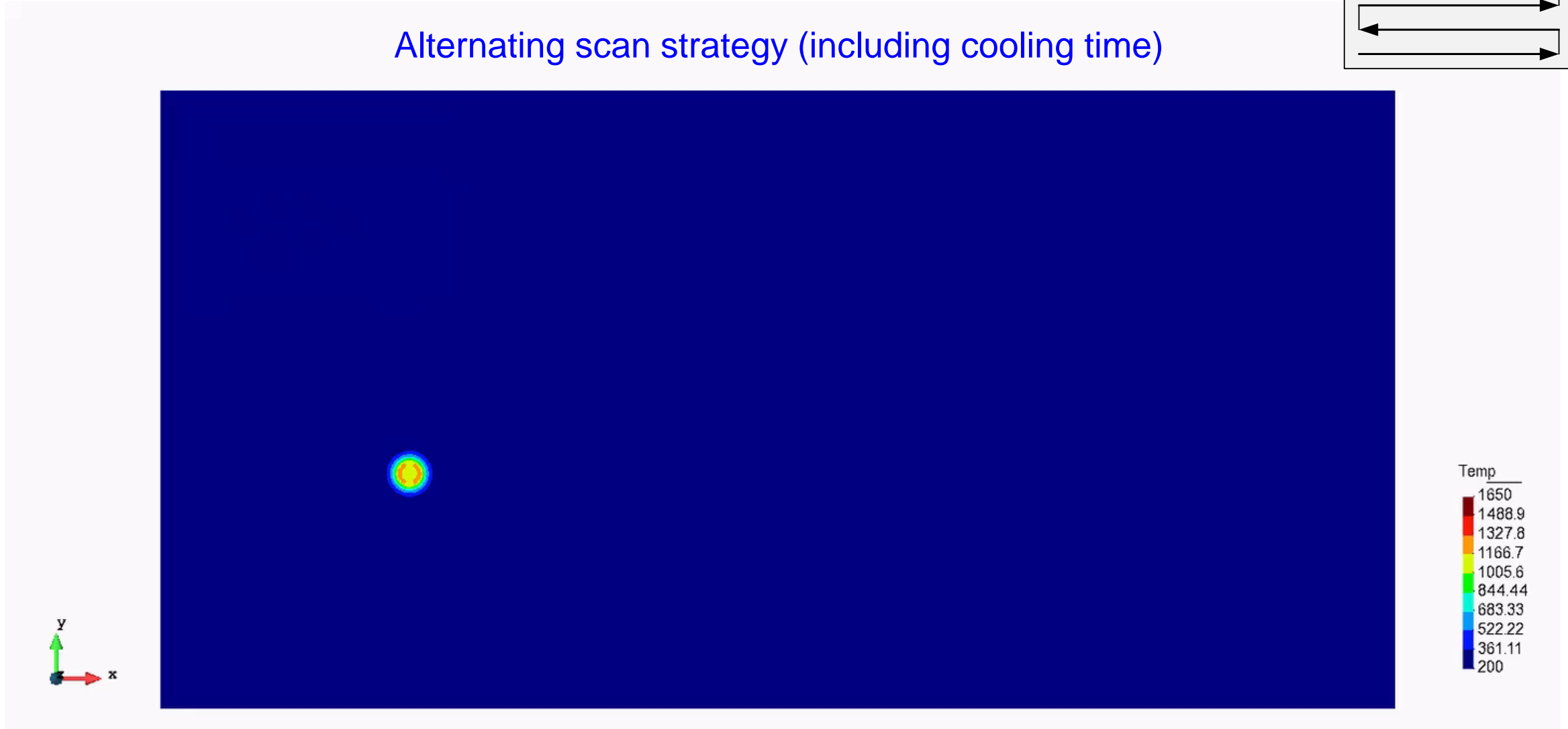
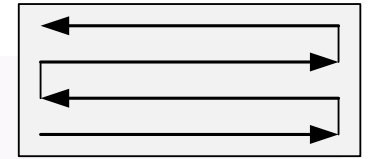
## Temperature field

Unidirectional scan strategy (including cooling time)



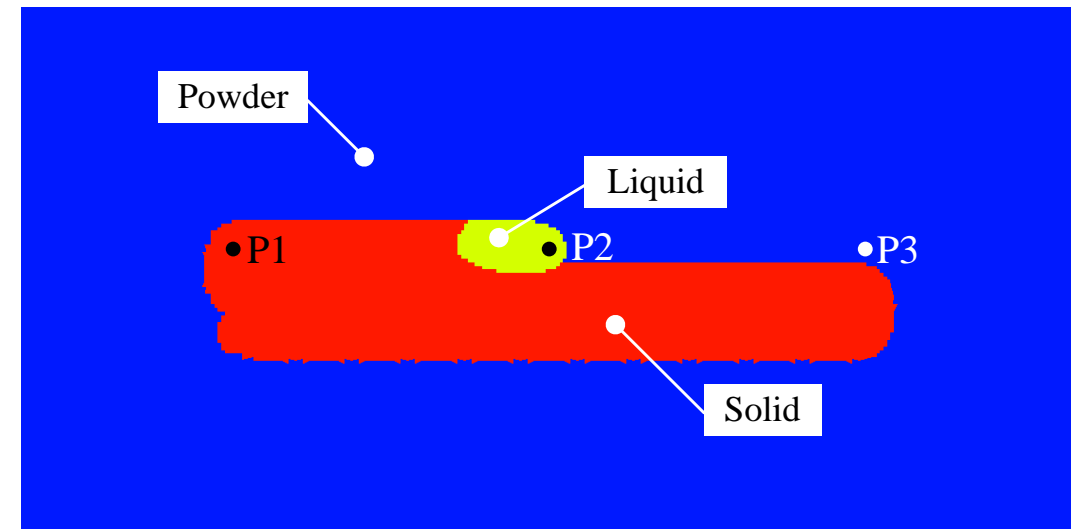
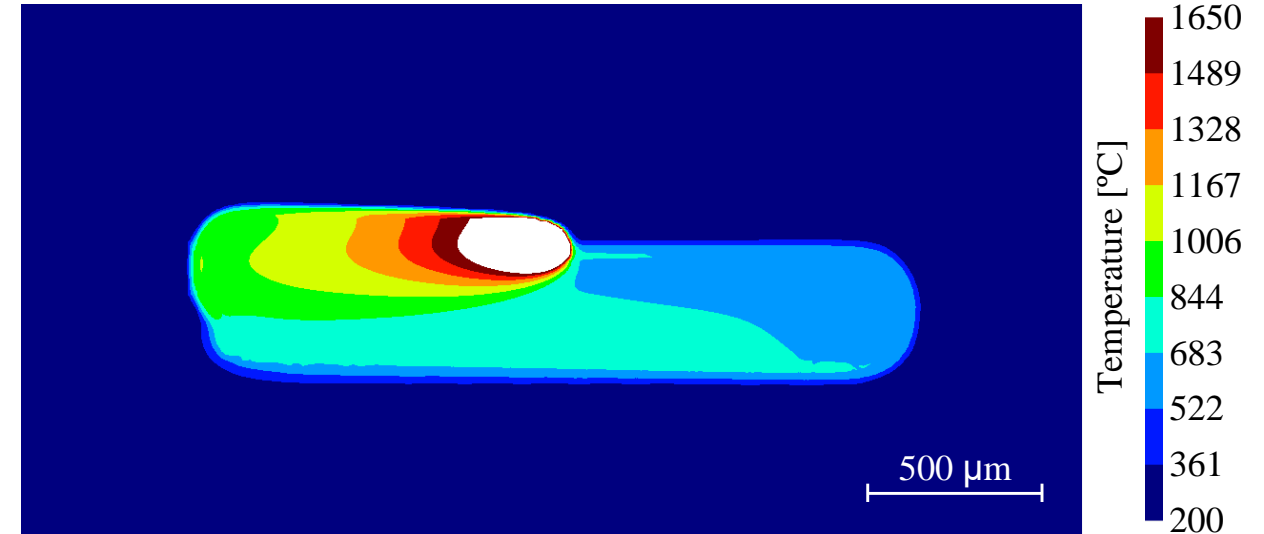
## Temperature field

Alternating scan strategy (including cooling time)



## Temperature field

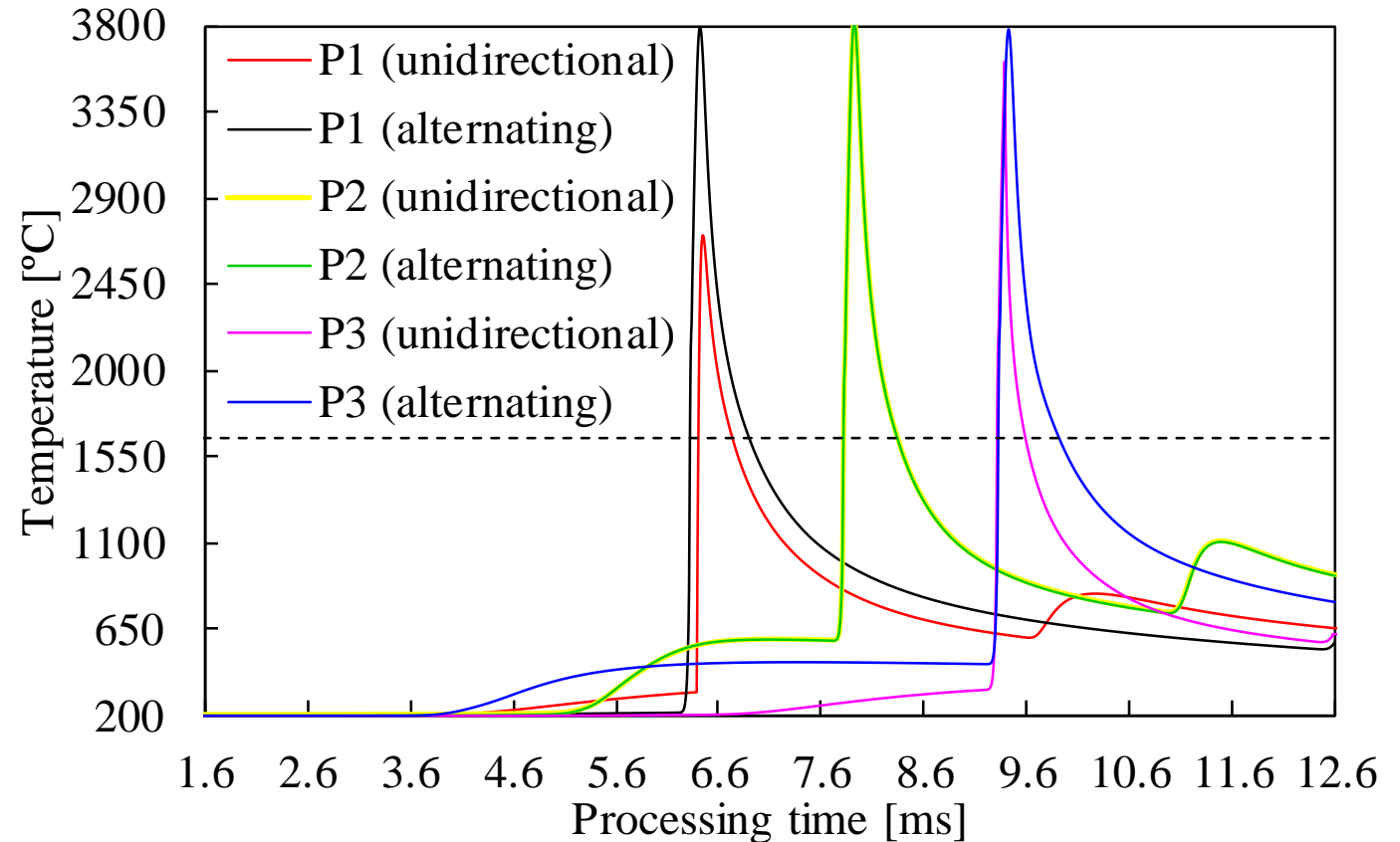
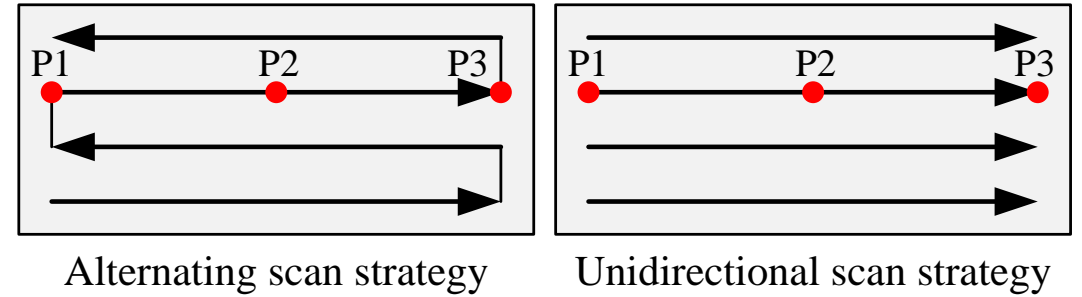
- Predicted **temperature field** when the laser beam is over P2 (alternating scan strategy)
- **Asymmetric temperature distribution** around the melt pool due to the low thermal conductivity of the powder
- The geometry of the melt pool is approximately semielliptical
- **Material phase status** defined by the thermal history of each finite element, using the melting temperature as bound





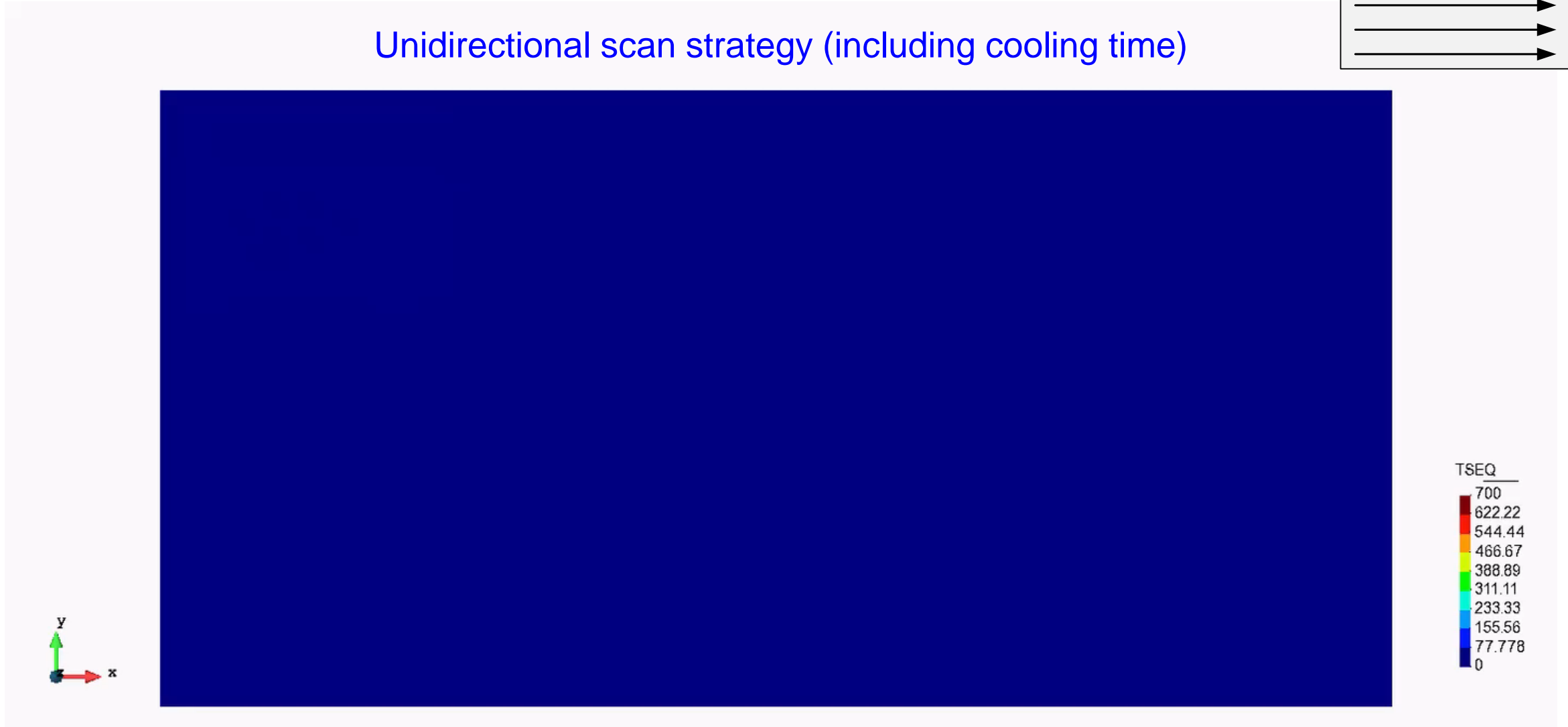
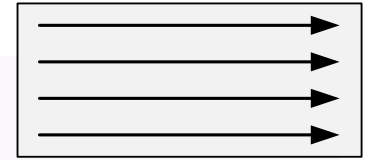
## Temperature field

- The peak temperature ( $\sim 3800^{\circ}\text{C}$ ) is a singularity inside the melt pool region
- Temperature evolution in **P2** is **independent of the scanning strategy**
- The cooling down rate is identical in all points using the **alternating scan strategy**
- Larger cooling down rate at the end of the scan vector using the **unidirectional scan strategy**



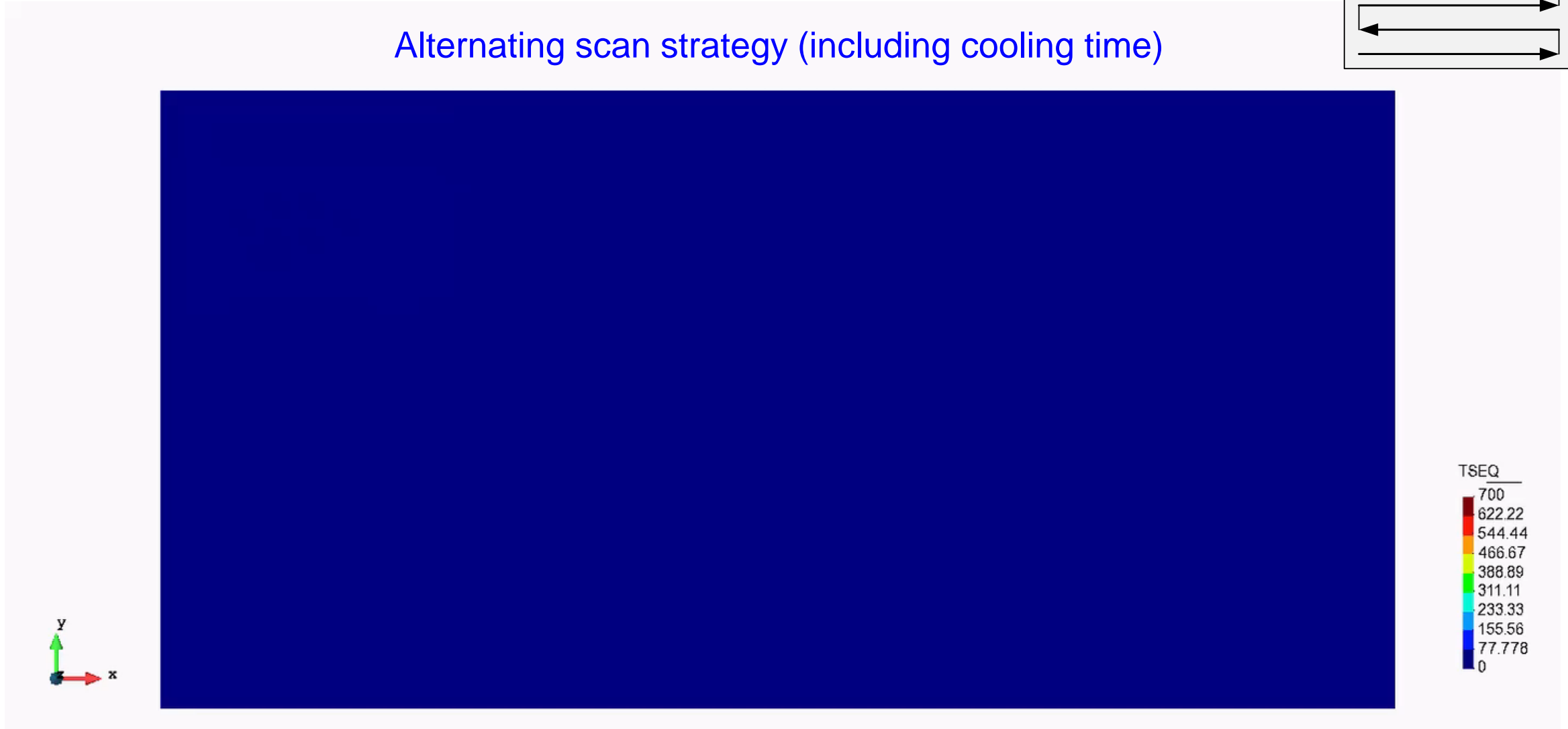
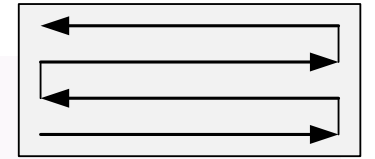
## Residual stress (von Mises)

Unidirectional scan strategy (including cooling time)



## Residual stress (von Mises)

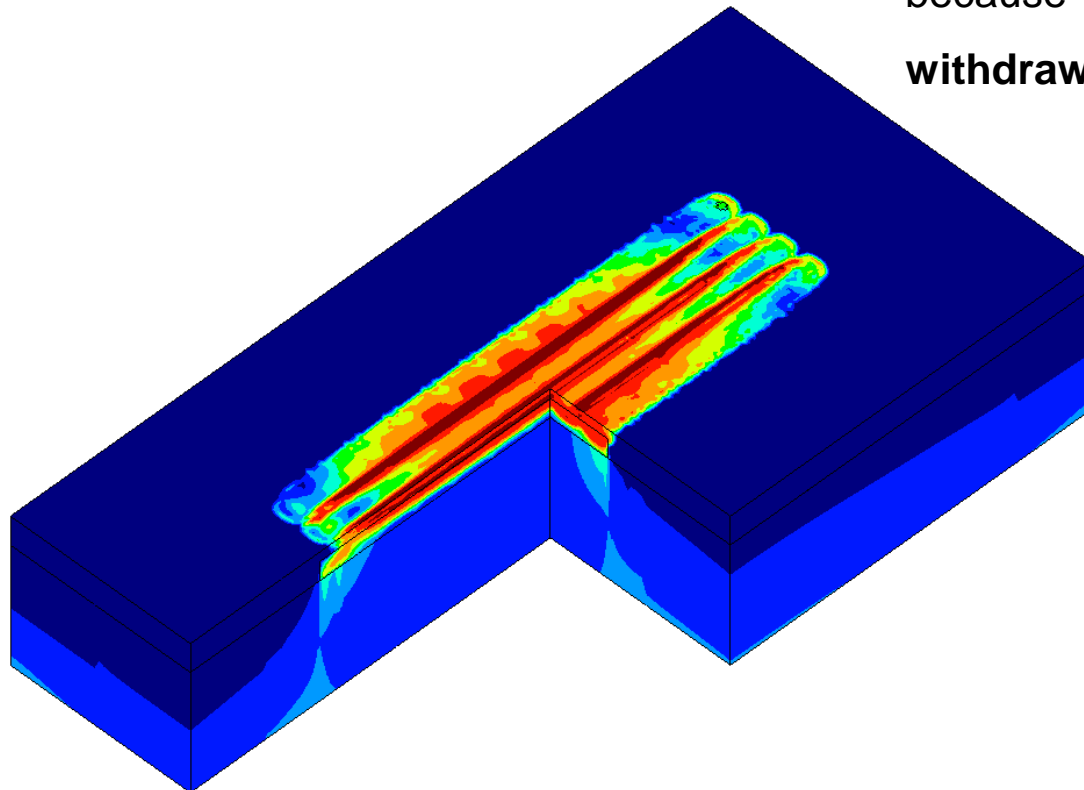
Alternating scan strategy (including cooling time)



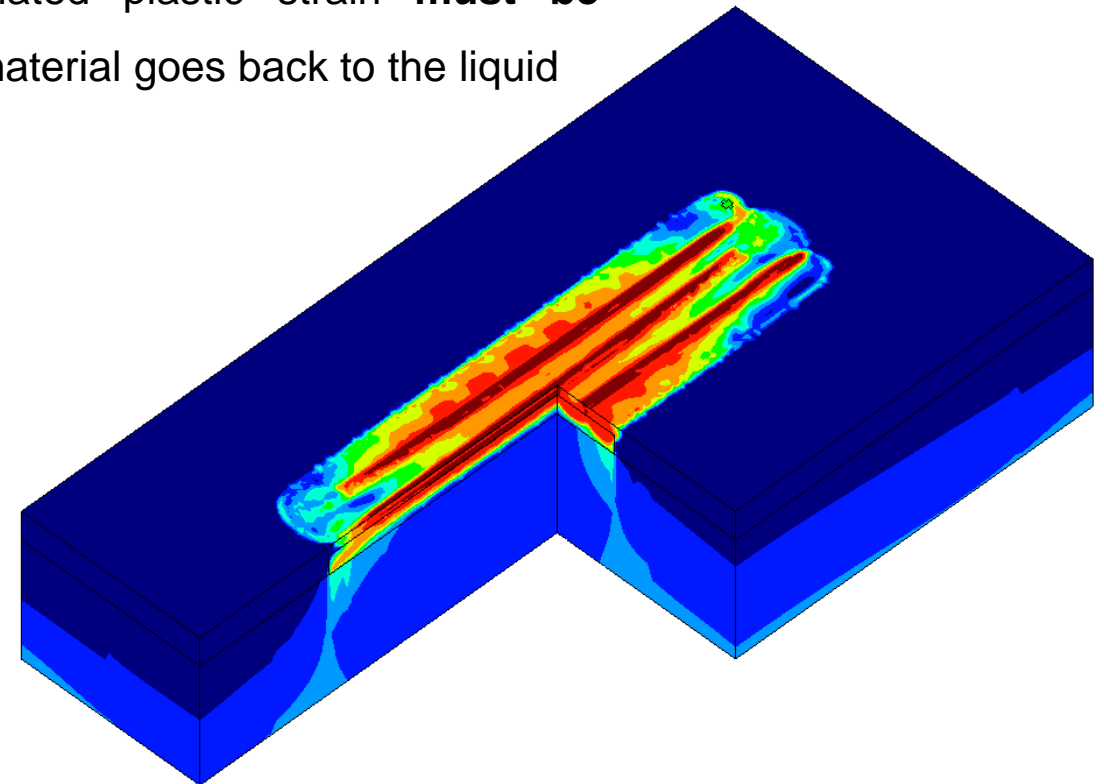
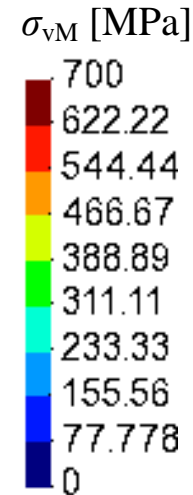
## Residual stress (von Mises)

- Distribution of the **von Mises equivalent stress** in the built component after **0.5 seconds of cooling time**

Increase of the stress in the overlapping scan tracks because the accumulated plastic strain **must be withdrawn** when the material goes back to the liquid



Unidirectional scan strategy

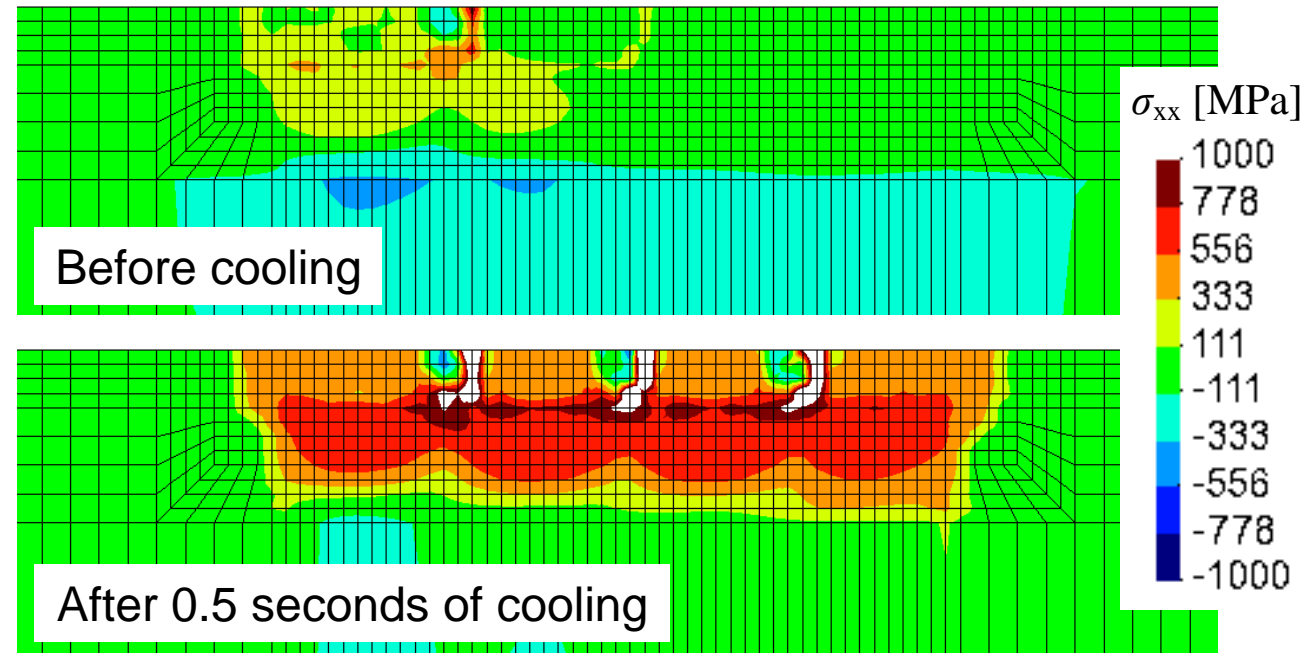
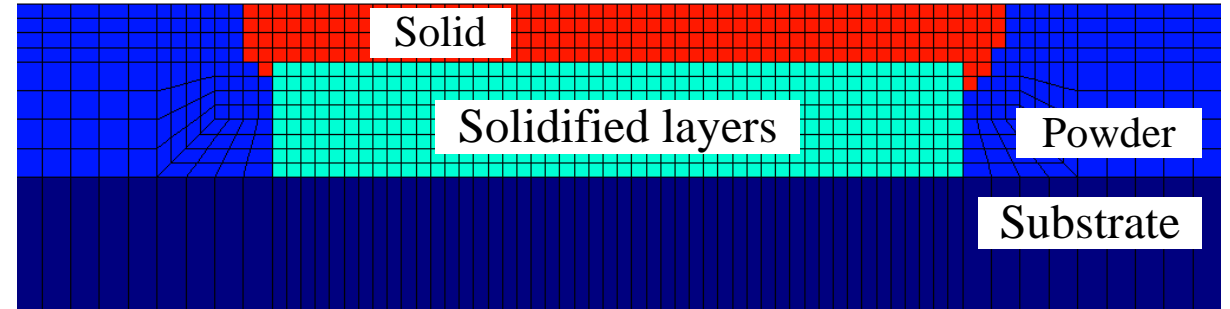


Alternating scan strategy

## Residual stress (von Mises)

- **Largest stress** component arises in the direction parallel to the scanning direction
- The **longitudinal residual stress** increases considerably during the cooling
- **Positive (tension) residual stresses** in the solidified layers
- Negligible impact of the **laser scan strategy** on the residual stress field

Transverse cross-section corresponding to the half-length (unidirectional scan strategy)

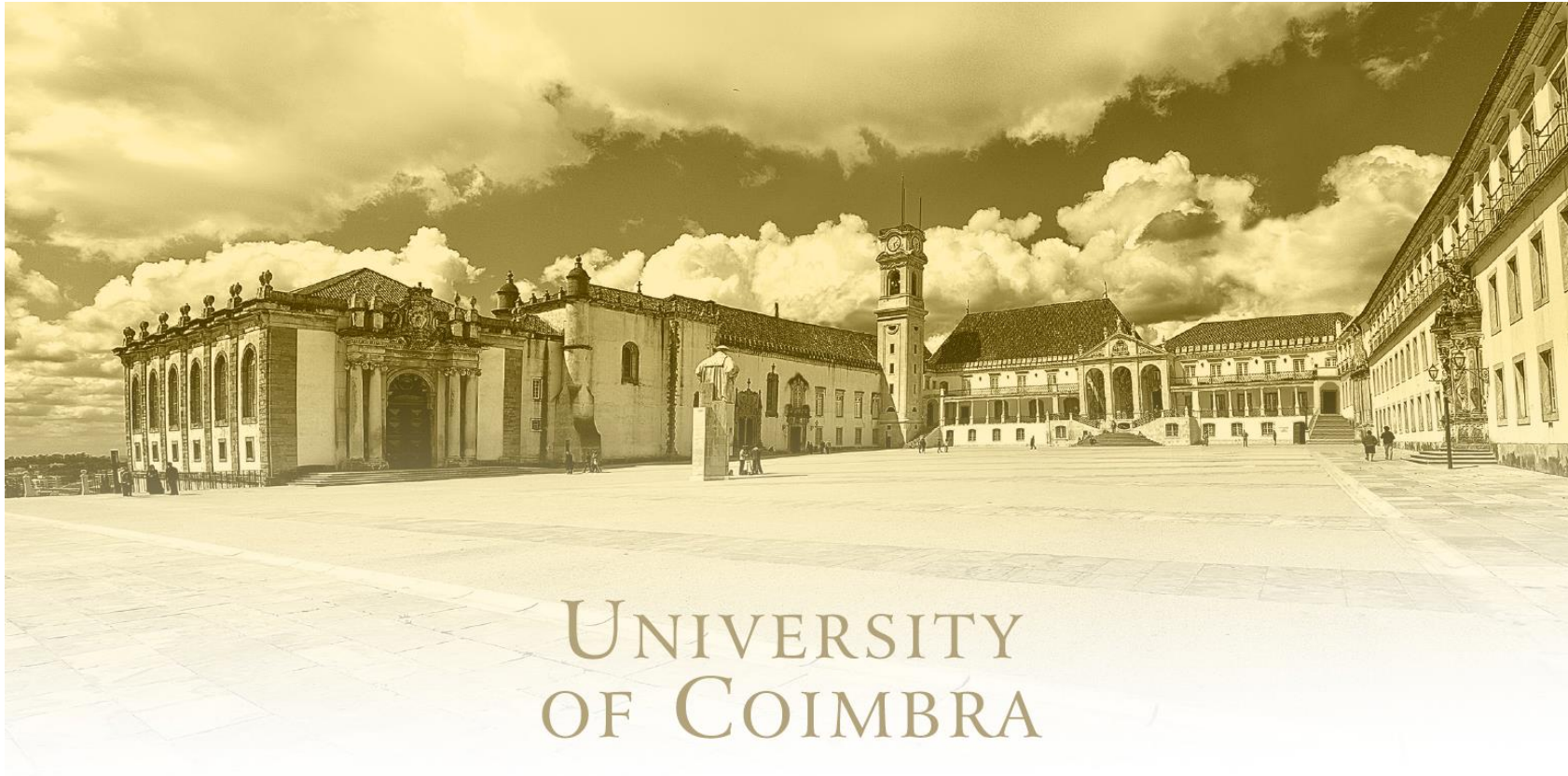


- **Finite element analysis** of the **selective laser melting** using a coupled **thermo-mechanical model** at meso-scale (**multi-track** in a **single powder layer** deposition)
- Transient thermal analysis and quasi-static mechanical analysis using **temperature dependent material properties**
- Influence of two different **laser scanning strategies** on the predicted residual stress
- **Shape and dimensions of the melt pool** estimated based on the predicted temperature distribution
- The residual stresses in the finished part are a result of the **non-uniform thermo-mechanical properties** (powder-liquid-solid)
- The **largest residual stress component** arises in the direction parallel to the scanning, which is **positive (tension)** in the solidified layers
- **Negligible effect of the laser scanning strategy** on the predicted stress, particularly at the mid-length of the scan vectors

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Projetos Cofinanciados pela UE:





**Thank you for watching!**