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# Influence of the orthotropic behaviour on defects prediction in cup drawing, reverse redrawing and expansions

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# Introduction

- The numerical simulation of cupping processes is fundamental for the can making industry.
- It allows the prediction of many different sheet metal defects and instabilities that significantly affect the efficient production of these parts.
- These defects include thinning from cup drawing, earing from plastic anisotropy, and damage and fracture from different combinations of strain paths, e.g. drawing and expansion.

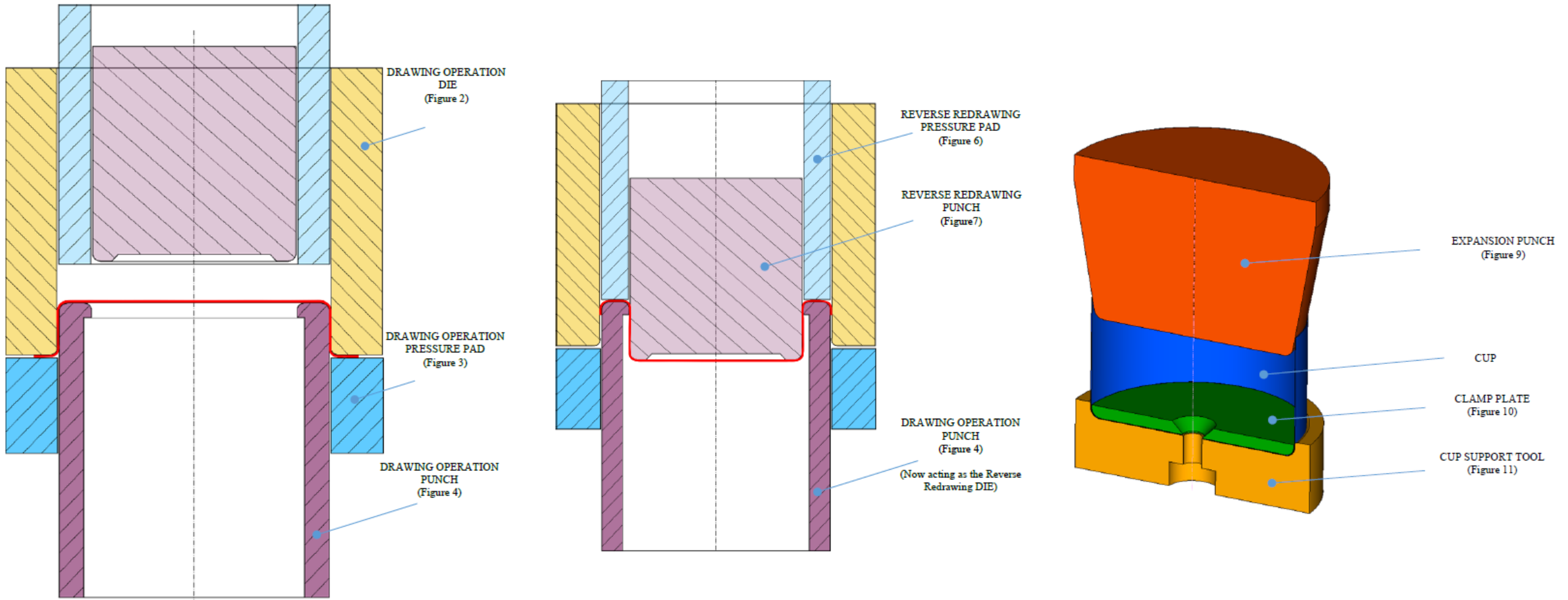


Alcoa Shaping Technology

Dick R, Finite Element Modeling Applications to Canmaking, Invited lecture at University of Coimbra, 2018).

# Forming defects prediction

## Benchmark 1 (Numisheet 2016): Benchmark 1 – Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion



Setup for the: Drawing operation (left) Reverse Redrawing operation (center) and Practical setup for the die expansion operation

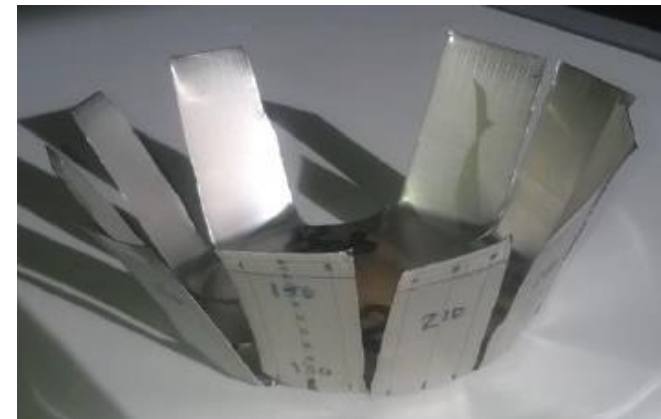
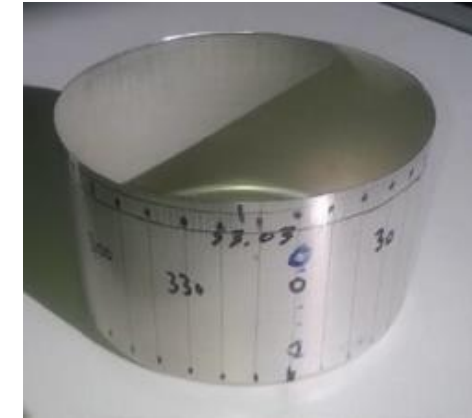
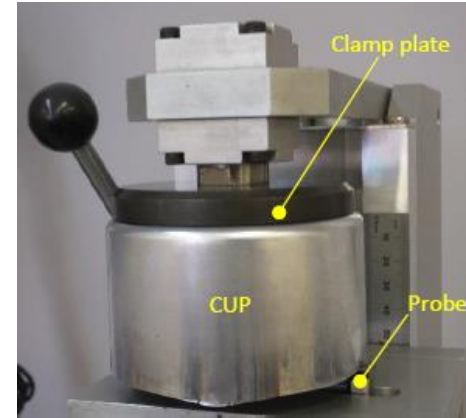
(Watson M, Dick R, Huang Y H, Lockley A, Cardoso R and Santos A 2016 Benchmark 1 - Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion J. Phys. Conf. Ser. 734 022001).

# Forming defects prediction

## Benchmark 1 (Numisheet 2016): Benchmark 1 – Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion

Steel cup

Aluminium cup



Cups after drawing and reverse redrawing (top-left); cups after expansion (bottom-left) and setups for earring and thickness measurements

(Watson M, Dick R, Huang Y H, Lockley A, Cardoso R and Santos A 2016 Benchmark 1 - Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion J. Phys. Conf. Ser. 734 022001).

## Benchmark 1 (Numisheet 2016): Benchmark 1 – Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion

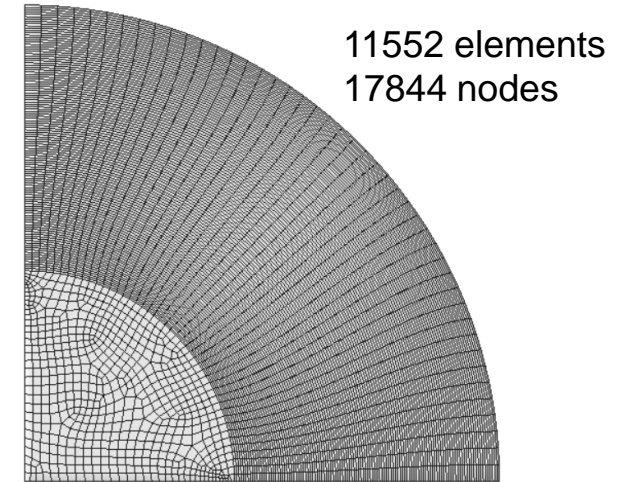
- The aims where the prediction:
  - of the earing, after the reverse redrawing operation;
  - of the thickness profile, after the reverse redrawing operation; and
  - of the failure point during the expansion operation.
- The blank sheet is circular with a diameter of 162.97 mm. Two materials with distinct orthotropic behaviour:
  - TH330 steel, with a thickness of 0.270 mm; and
  - AA5352 aluminium alloy, with a thickness of 0.279 mm.
- The drawing and reverse redrawing operations are performed considering a constant pressure-pad force, which is also equal for both materials:
  - Drawing operation: 21.1 kN; and
  - Redrawing: 16.6 kN.
- Recommend value for the constant friction coefficient of 0.03.



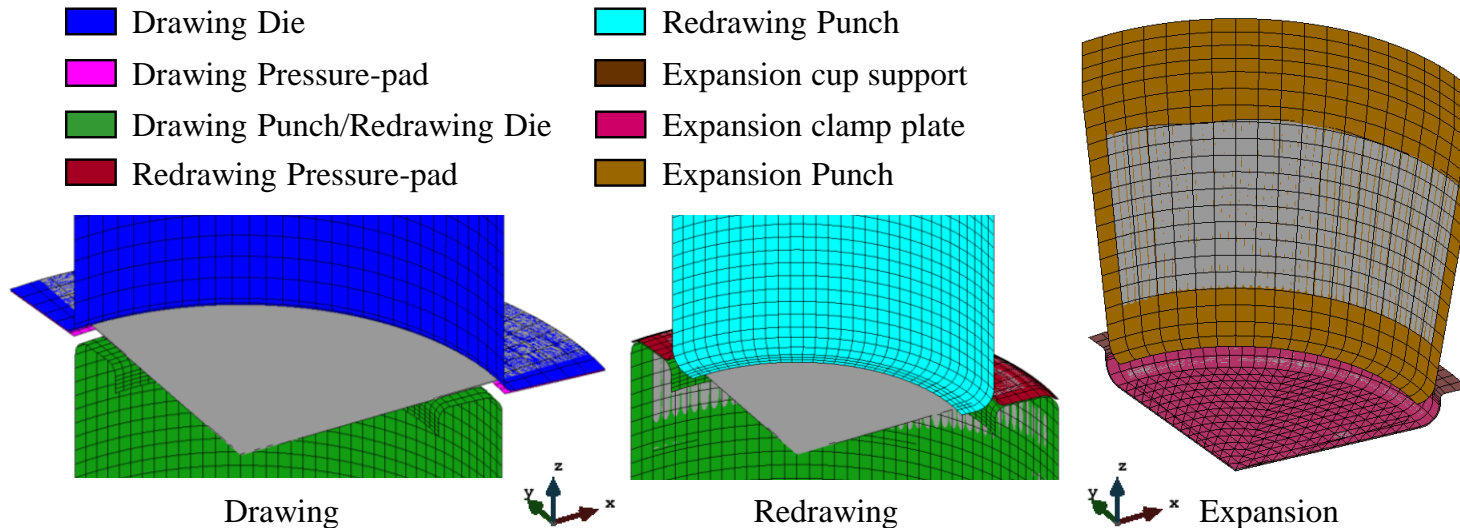
# Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion

## Finite element model

- DD3IMP in-house finite element code (implicit time integration)
- 1/4 of the model (symmetry conditions)
- Forming tools are assumed rigid discretized by Nagata patches
- The Coulomb friction law is adopted, constant  $\mu = 0.03$
- Blank discretized by linear hexahedral (8-nodes) finite elements (2 layers through the thickness)



Discretization of the blank with hexahedral finite elements.

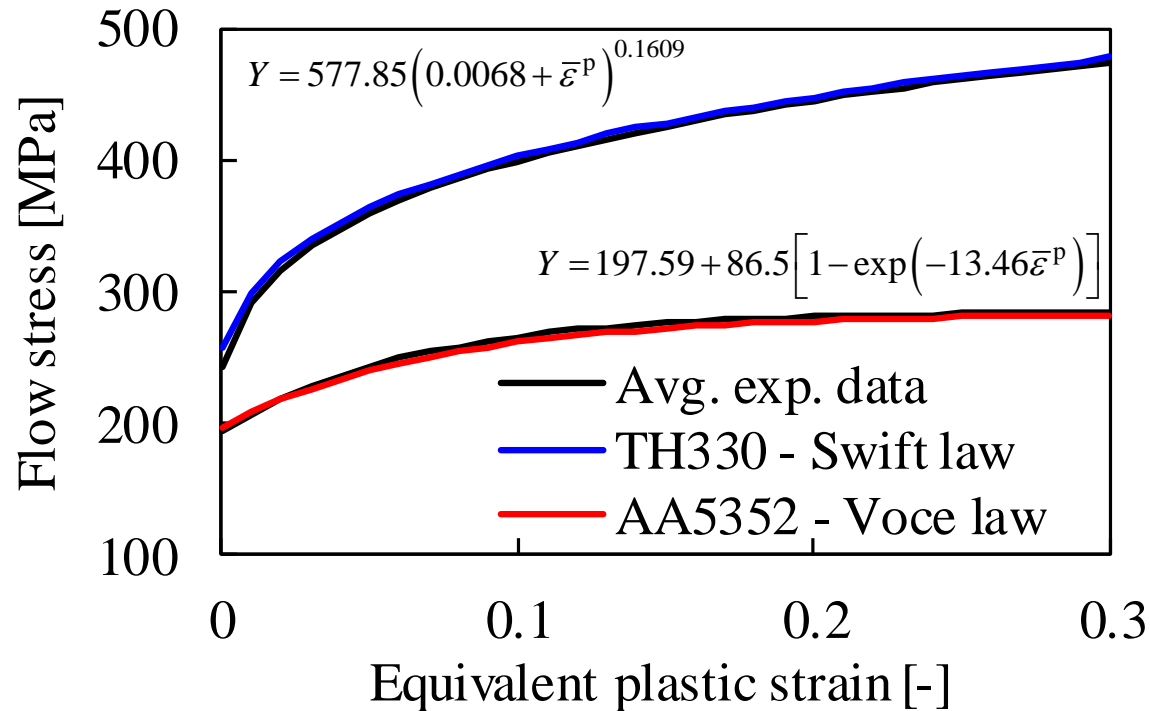


Numerical model: Nagata patches used to describe the surfaces of each tool.

# Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion

## Finite element model

- Isotropic elastic behaviour described with the Hooke's law.
- Isotropic hardening law determined by best fit for the stress-plastic strain curve, from the uniaxial test performed in the rolling direction (RD).



Stress–equivalent plastic strain curve and hardening law fitted from the uniaxial tensile test in RD.

Test	TH330 steel		AA5352 aluminium	
	$r$	$\sigma_\theta/Y_0$	$r$	$\sigma_\theta/Y_0$
0°	1.449	1.000	0.535	1.000
15°	1.373	0.998	0.465	0.979
30°	1.301	0.983	0.655	0.995
45°	1.266	0.986	1.105	0.982
60°	1.335	0.971	1.415	0.997
75°	1.443	0.967	1.595	0.996
90°	1.510	0.963	2.270	1.006
Biaxial	0.984	1.198	0.620	1.225

$r$ -values and normalized yield stress values extracted from uniaxial tensile tests; biaxial stress extracted from bulge test and  $r_b$  extracted from disk compression test.

## Cazacu and Barlat, 2001 (CB2001)

$$(J_2^0)^3 - c(J_3^0)^2 = 27\left(\frac{Y}{3}\right)^6$$

$$J_2^0 = \frac{a_1}{6}(\sigma_{11} - \sigma_{22})^2 + \frac{a_2}{6}(\sigma_{11} - \sigma_{33})^2 + \frac{a_3}{6}(\sigma_{11} - \sigma_{33})^2 \\ + a_4\sigma_{12}^2 + a_5\sigma_{13}^2 + a_6\sigma_{23}^2$$

$$J_3^0 = (1/27)(b_1 + b_2)\sigma_{11}^3 + (1/27)(b_3 + b_4)\sigma_{22}^3 \\ + (1/27)[2(b_1 + b_4) - b_2 - b_3]\sigma_{33}^3 \\ - (1/9)(b_1\sigma_{22} + b_2\sigma_{33})\sigma_{11}^2 - (1/9)(b_3\sigma_{33} + b_4\sigma_{11})\sigma_{22}^2 \\ - (1/9)[(b_1 - b_2 + b_4)\sigma_{11} + (b_1 - b_3 + b_4)\sigma_{22}]\sigma_{33}^2 \\ + (2/9)(b_1 + b_4)\sigma_{11}\sigma_{22}\sigma_{33} \\ - (\sigma_{13}^2/3)[2b_9\sigma_{22} - b_8\sigma_{33} - (2b_9 - b_8)\sigma_{11}] \\ - (\sigma_{12}^2/3)[2b_{10}\sigma_{33} - b_5\sigma_{22} - (2b_{10} - b_5)\sigma_{11}] \\ - (\sigma_{23}^2/3)[(b_6 - b_7)\sigma_{11} - b_6\sigma_{22} - b_7\sigma_{33}] + 2b_{11}\sigma_{12}\sigma_{23}\sigma_{13}$$

Anisotropy parameters

$a_1, a_2, a_3, a_4$

$b_1, b_2, b_3, b_4, b_5, b_{11}$

Weighting coefficient

$c$



## DD3MAT: objective function

$$F(\mathbf{A}) = w_{\sigma_{\theta}} \sum_{\theta} \left( \sigma_{\theta}(\mathbf{A}, \bar{\varepsilon}^p) / \sigma_{\theta}(\bar{\varepsilon}^p) - 1 \right)^2 + w_{r_{\theta}} \sum_{\theta} \left( r_{\theta}(\mathbf{A}) / r_{\theta} - 1 \right)^2 \\ + w_{\sigma_b} \left( \sigma_b(\mathbf{A}, \bar{\varepsilon}^p) / \sigma_b(\bar{\varepsilon}^p) - 1 \right)^2 + w_{r_b} \left( r_b(\mathbf{A}, \bar{\varepsilon}^p) / r_b(\bar{\varepsilon}^p) - 1 \right)^2$$

$\mathbf{A}$  – set of anisotropy parameters

$\sigma_{\theta}$  – yield stresses in uniaxial tension

$r_{\theta}$  – anisotropy coefficients in uniaxial tension

$\sigma_b$  – yield stresses in biaxial tension

$r_b$  – anisotropy coefficient in biaxial compression

$w_i$  – weighting coefficients

- Minimized with a downhill simplex method.
- First approach: anisotropy parameters identified considering a similar weighting factor for all experimental data.
- For the AA5352 aluminium alloy, another identification performed, increasing the weight for the biaxial yield stress.

# Orthotropic behaviour

## Identification of the anisotropy parameters

- **TH330 steel:** Based on the  $r$ -value and yield stress in-plane directionalities and on biaxial values.

$c$	$a_1$	$a_2$	$a_3$	$a_4$	$b_1$	$b_2$	$b_3$	$b_4$	$b_5$	$b_{10}$	Others
0.79	1.315	0.91	0.874	1.089	2.037	1.184	1.02	0.849	0.454	0.702	1.00000

- **AA5352 aluminium:** Based on the  $r$ -value and yield stress in-plane directionalities and on biaxial values.

- With equal weighting values

$c$	$a_1$	$a_2$	$a_3$	$a_4$	$b_1$	$b_2$	$b_3$	$b_4$	$b_5$	$b_{10}$	Others
0.91	1.09	0.86	1.065	0.98	2.95	0.323	3.104	-1.804	-1.055	0.658	1.00000

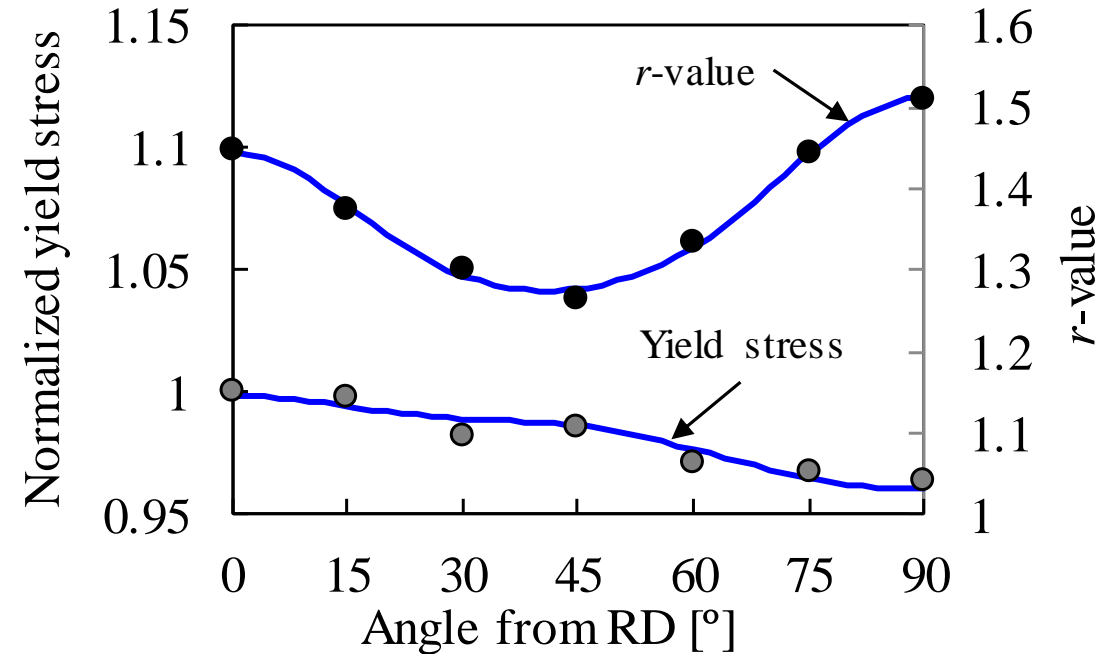
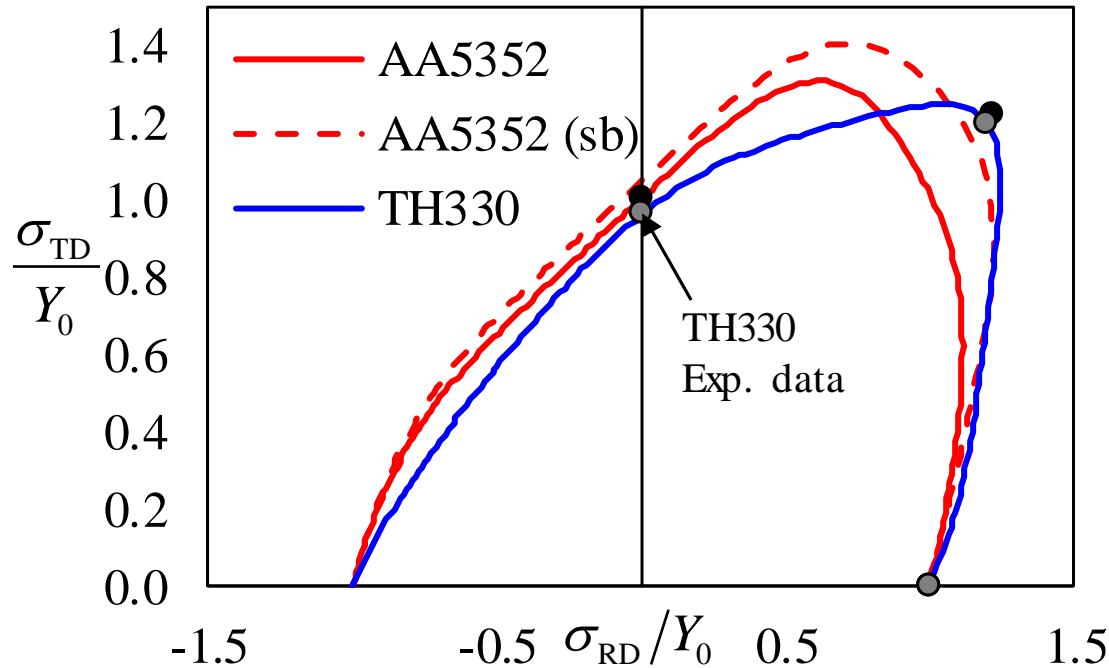
- With an higher weighting value for the biaxial stress

$c$	$a_1$	$a_2$	$a_3$	$a_4$	$b_1$	$b_2$	$b_3$	$b_4$	$b_5$	$b_{10}$	Others
1.532	1.293	0.527	0.992	0.868	2.944	-0.005	1.704	-1.882	-1.17	0.244	1.00000

# Orthotropic behaviour

## Identification of the anisotropy parameters

- For the TH330 steel, the CB2001 recovers quite well the biaxial yield stress (experimental value of 310 MPa and analytical value of 306.8 MPa), the  $r_b$  (experimental value of 0.984 and analytical of 0.983), as well as the results from the uniaxial tensile tests.

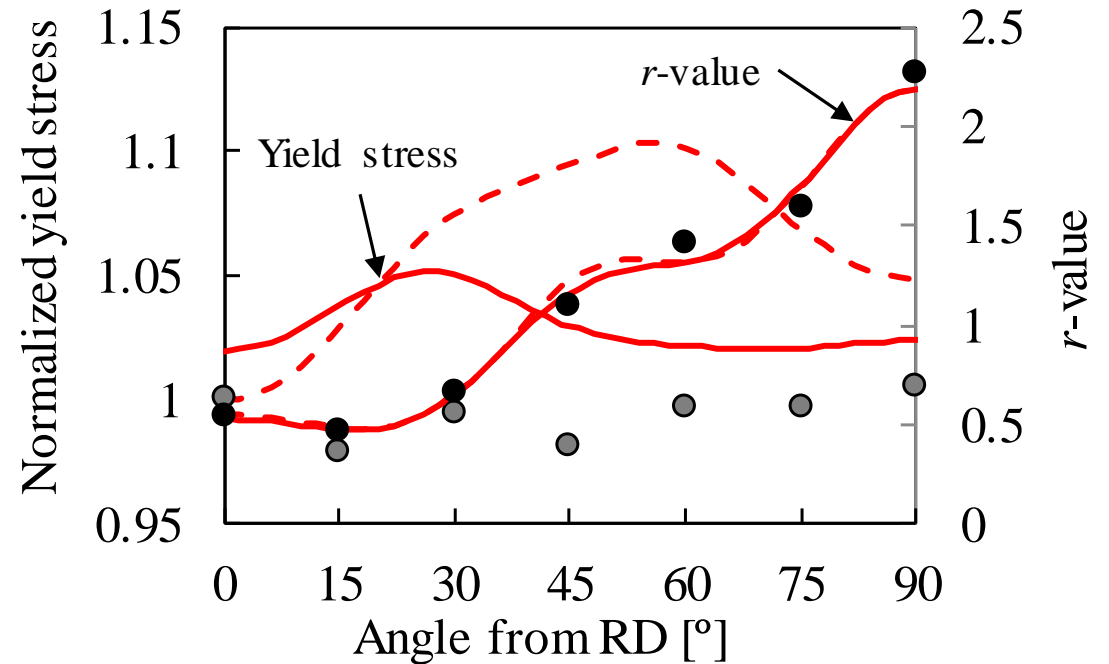
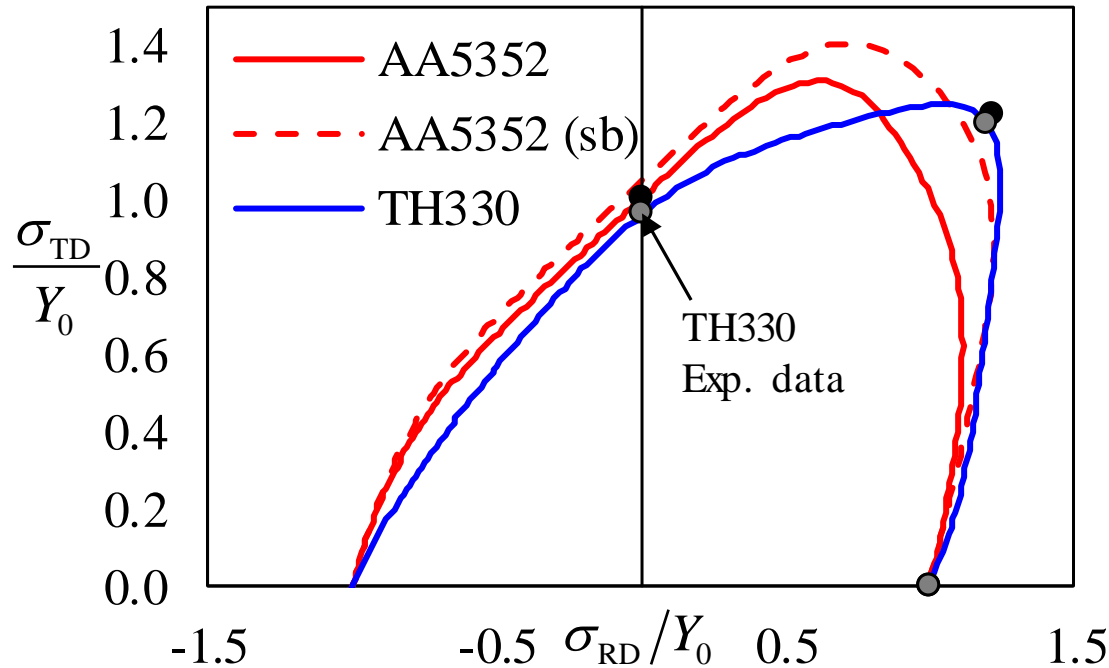


Projection of the yield surface in the biaxial plane (left) and experimental and predicted  $r$ -values and yield stresses for the TH330 steel.

# Orthotropic behaviour

## Identification of the anisotropy parameters

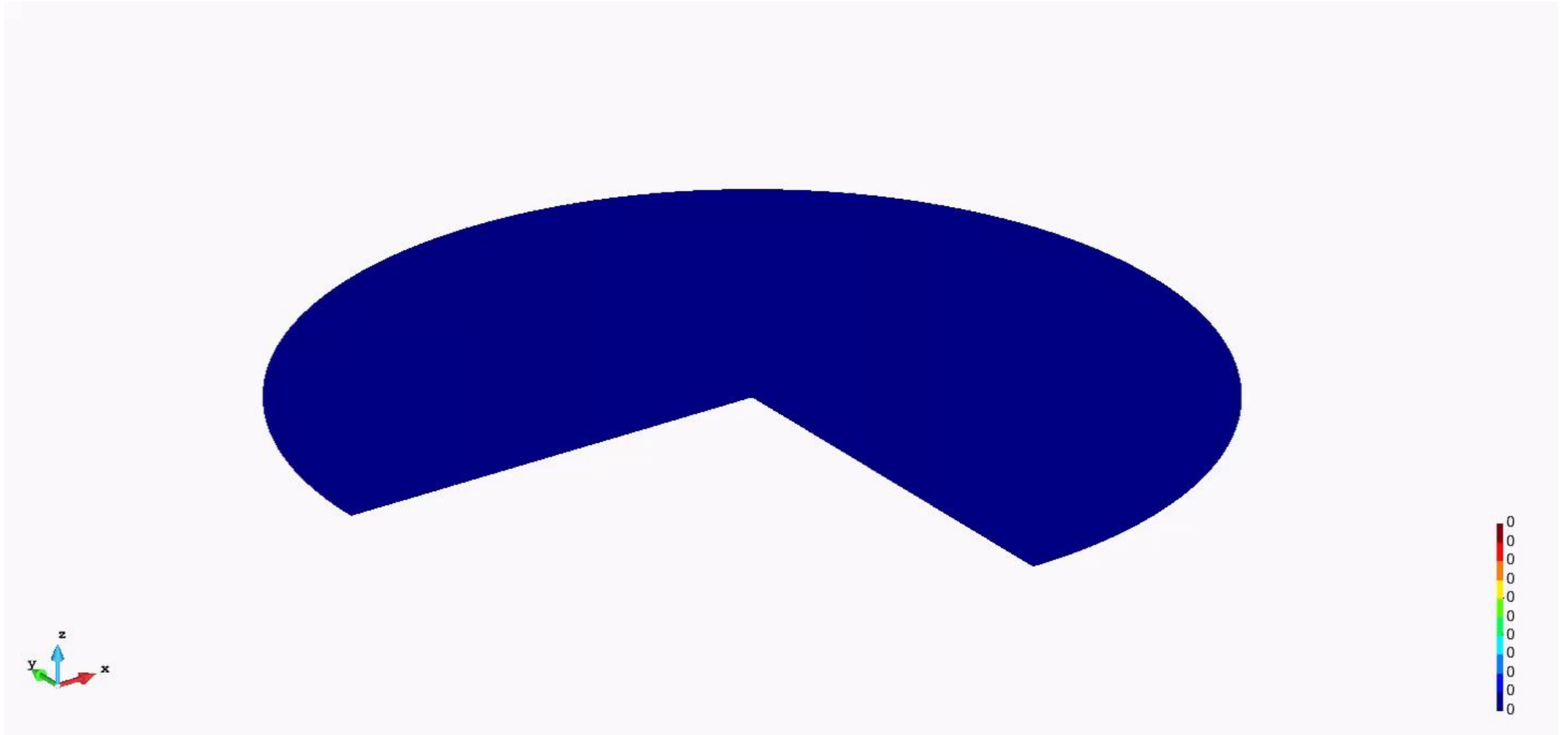
- For the AA5352 aluminium alloy, the CB2001 only recovers quite well the biaxial yield stress (experimental value of 242.01 MPa and analytical value of 227.61 MPa), the  $r_b$  (experimental value of 0.620 and analytical of 0.643), when the weight for the biaxial value is increased.



Projection of the yield surface in the biaxial plane (left) and experimental and predicted  $r$ -values and yield stresses for the AA5352 aluminium.

# Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion

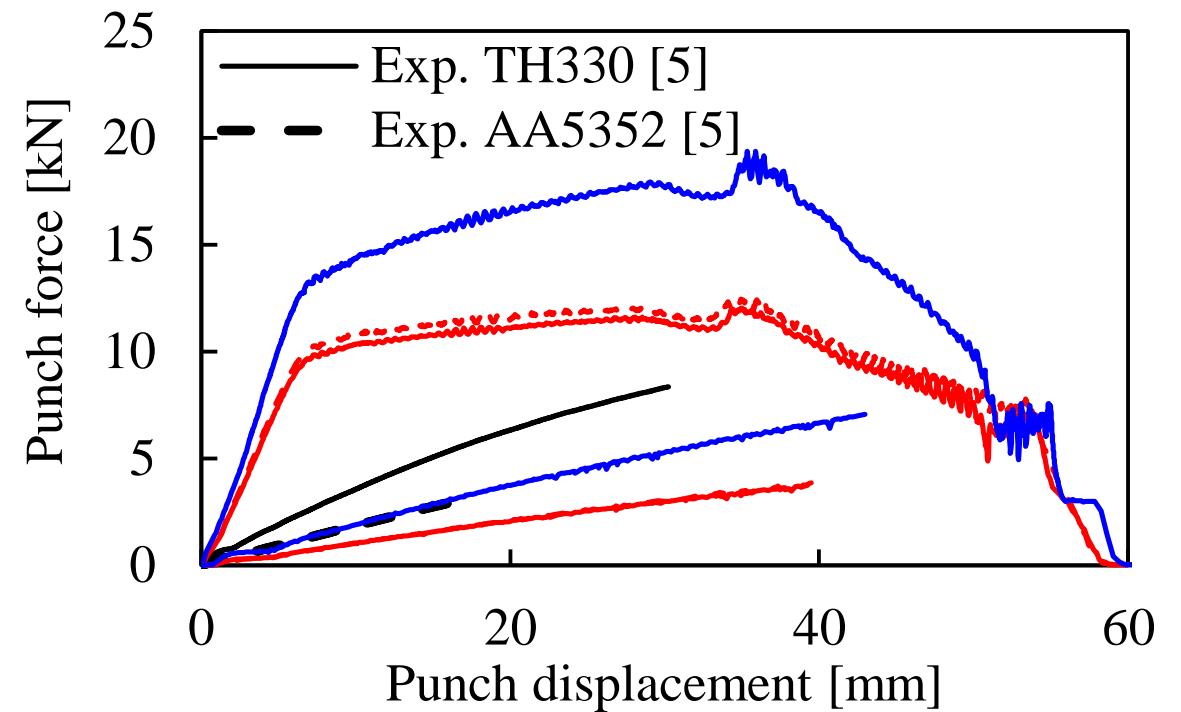
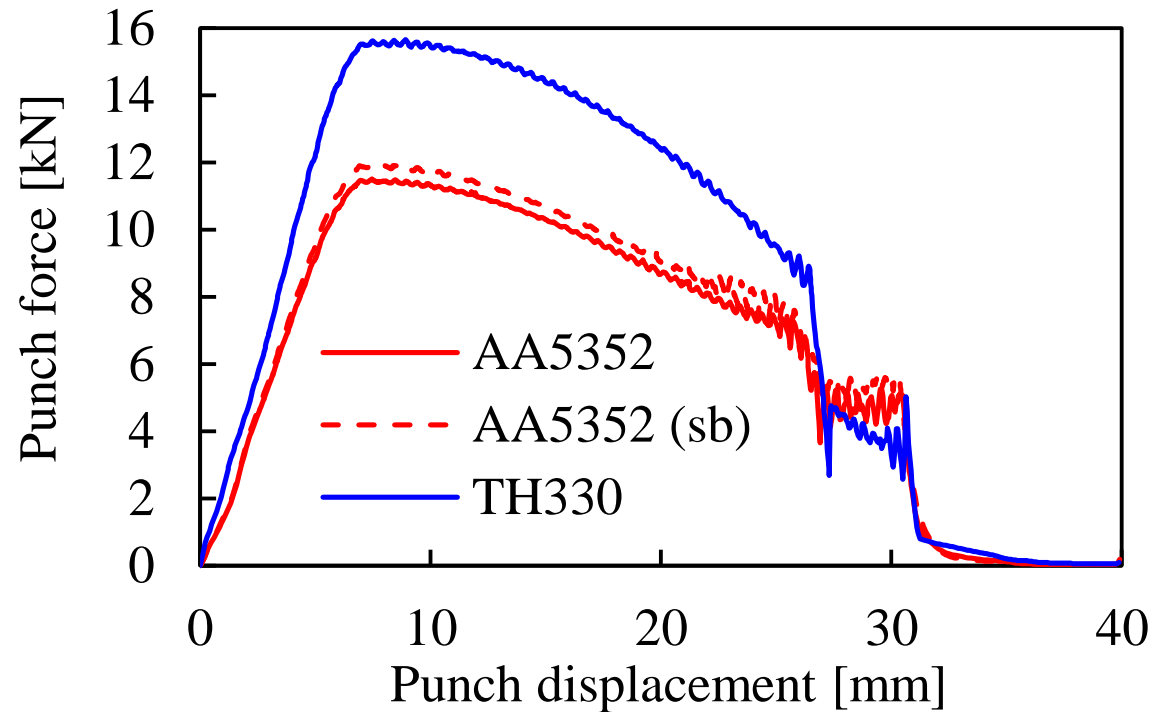
Finite element model: AA5352 aluminium



# Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion

## Drawing force

- The “AA5352 (sb)” results in slightly higher values of force than for “AA5352”, which can be related with the globally higher yield stress in-plane directionalities.
- The expansion punch force presents a linear trend with its stroke, which is clearly underestimated, for both materials.



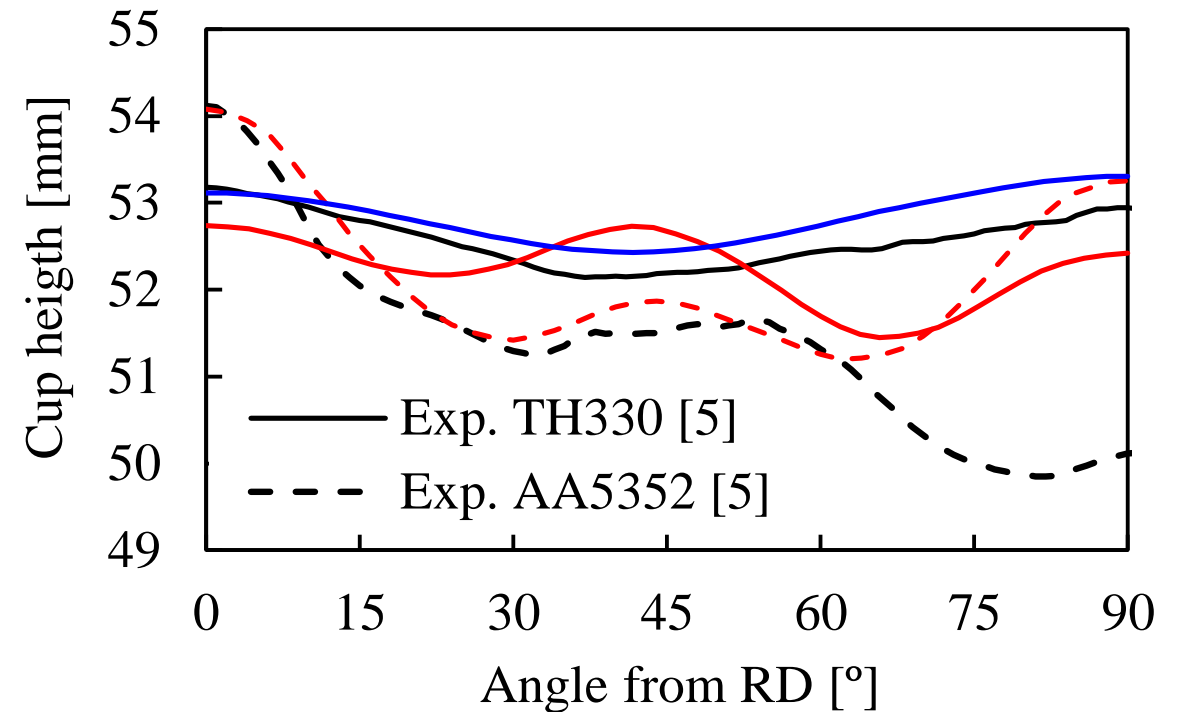
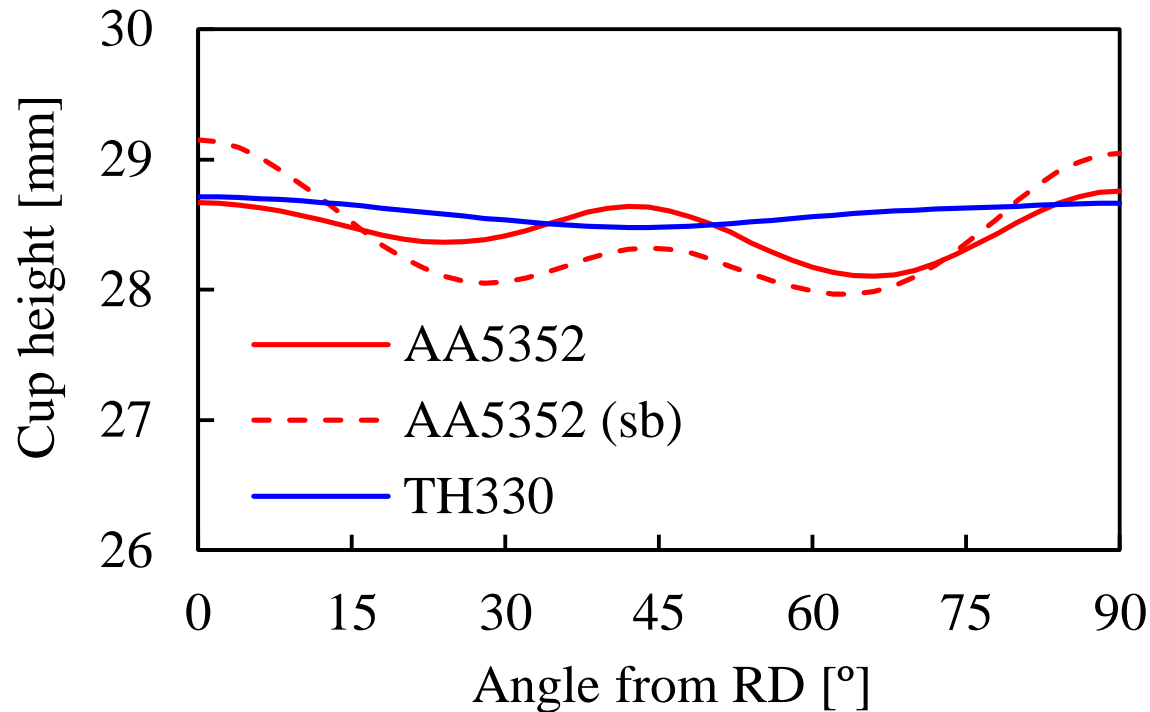
Comparison between experimental measurement and numerical prediction of the punch force evolution with the displacement in the drawing (left) and reverse redrawing and expansion (right).



# Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion

## Earing profile

- The TH330 steel presents an almost constant height, with 4 ears more visible after redrawing.
- The AA5352 aluminium alloy presents a total of 8 ears, which have a higher amplitude for the “AA5352 (sb)”. However, the trend for the height is not well captured, because at TD it is clearly overestimated, by both sets of anisotropy parameters.

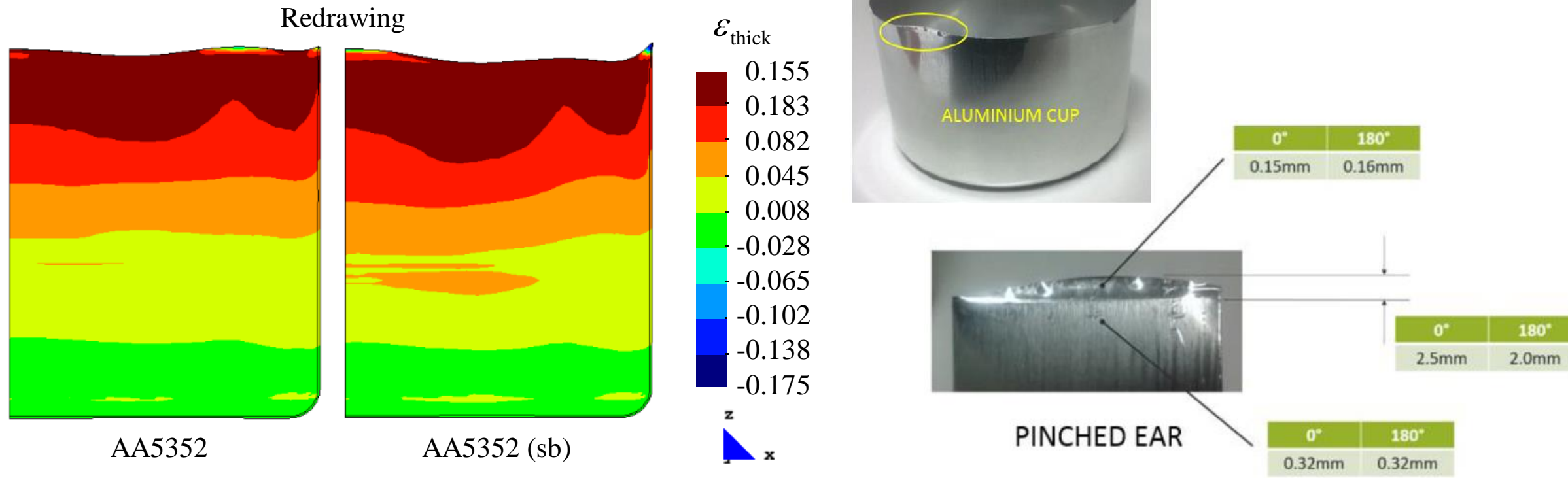


Comparison between experimental and predicted up height, in function of the angle from RD, at the end of the drawing (left) and reverse redrawing (right).

# Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion

## Earing profile

- For the AA5352 aluminium alloy, at the end of the reverse redrawing stage there are some areas with strong thinning at the top of the cup. For “AA5352” this occurs at the RD and close to 45° with RD, while for “AA5352 (sb)” it disappears for 45° but appears at TD, and becomes more relevant at the RD.

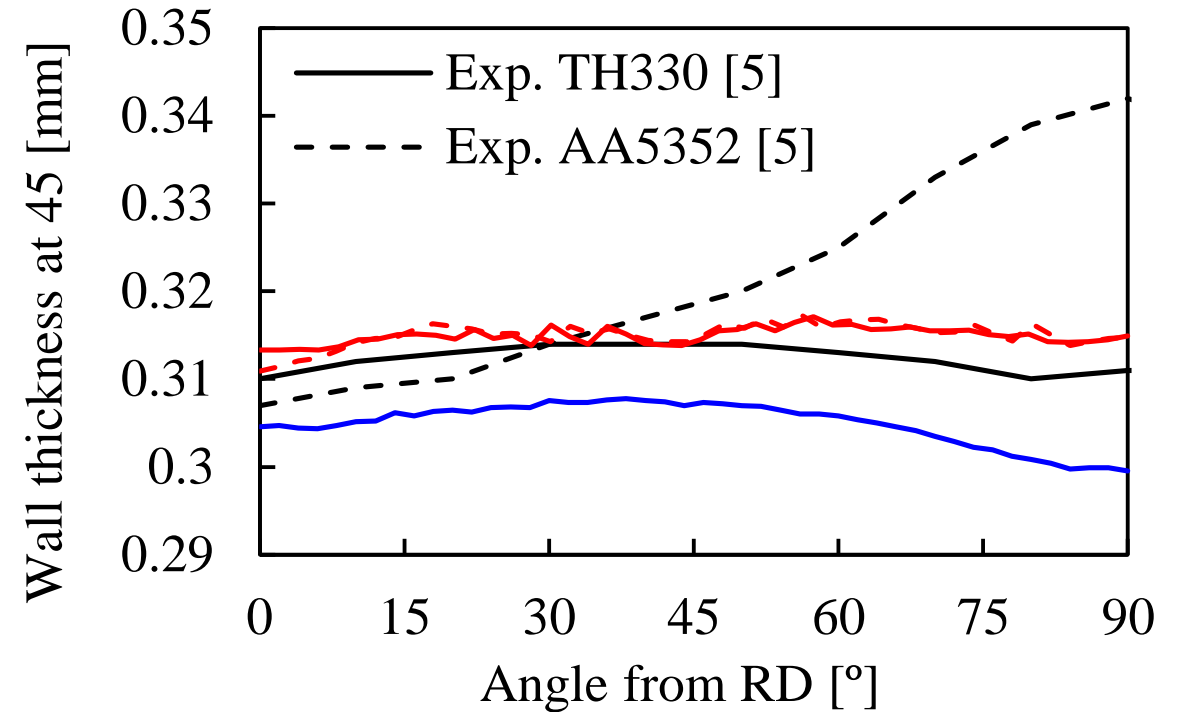
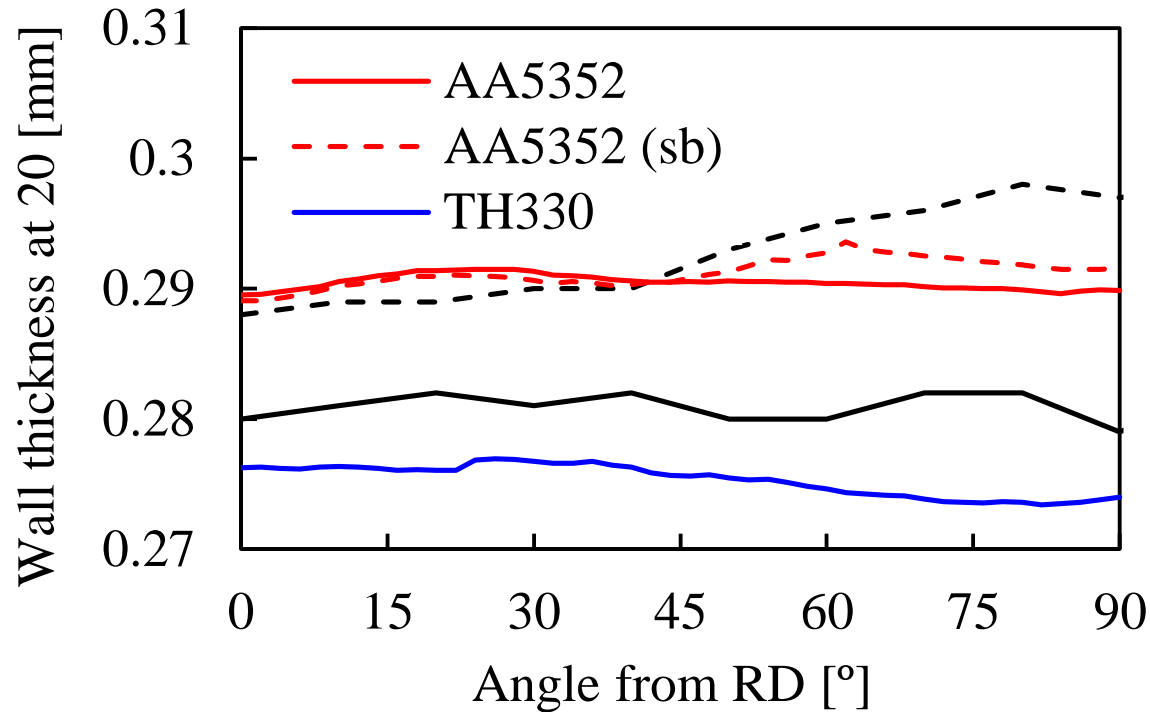


Distribution of the thickness strain at the end of the reverse redrawing, for the AA5352 aluminium alloy (left) and experimental analysis of the location of the pinched ears (right).

# Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion

## Thickness distribution

- For the TH330 steel, the numerical values are always below the experimental range.
- For the AA5352 aluminium alloy, the numerical values are close to the minimum value of the experimental range. Moreover, the experimental results present an increasing trend between RD and TD, while the numerical are almost constant value. Note that there was some ironing of the vertical wall during the redrawing stage.

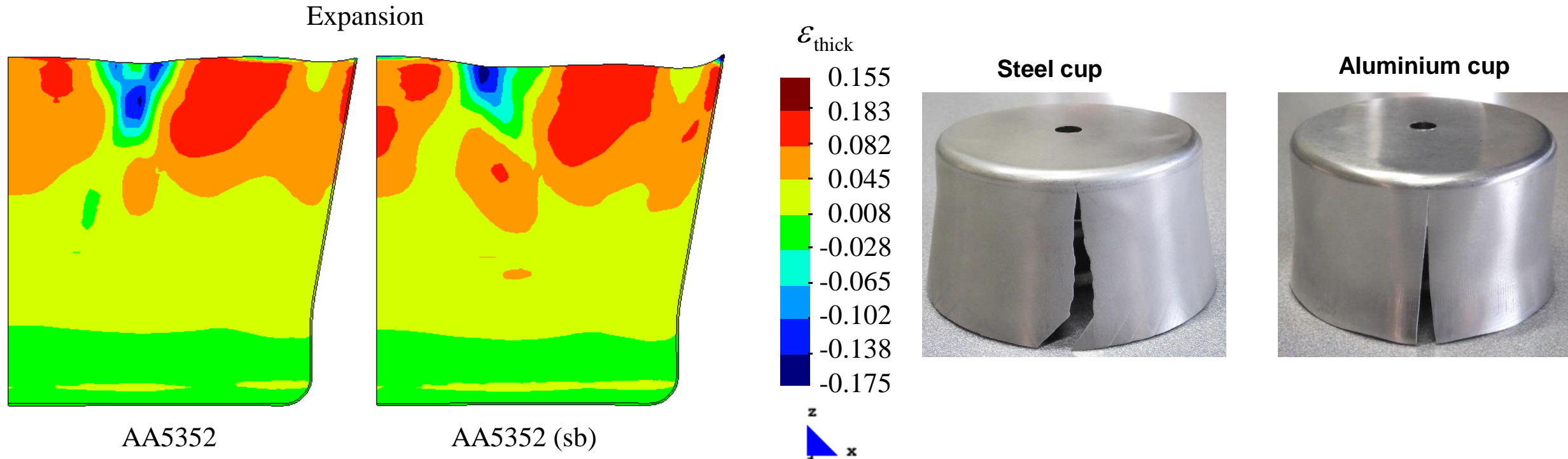


Comparison between experimental and predicted results for the wall thickness in function of the angle from RD, at the end of the reverse redrawing operation, at a distance from the cup base of 20 mm (left) and 45 mm (right).

# Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion

## Fracture during expansion

- For the TH330 steel, there is no strain localization in the part.
- For the AA5352 aluminium alloy, the strain localization is predicted by both sets of anisotropy parameters, for similar displacements of the expansion punch and at identical orientations with RD. Both numerical results overestimate the punch displacement and the location is not that close to TD.

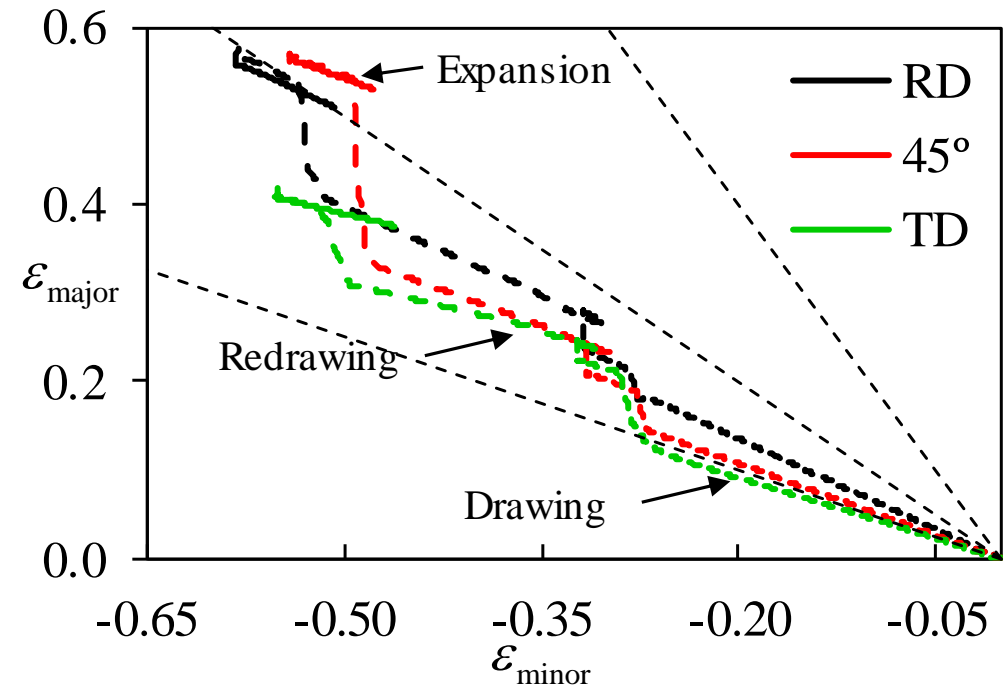
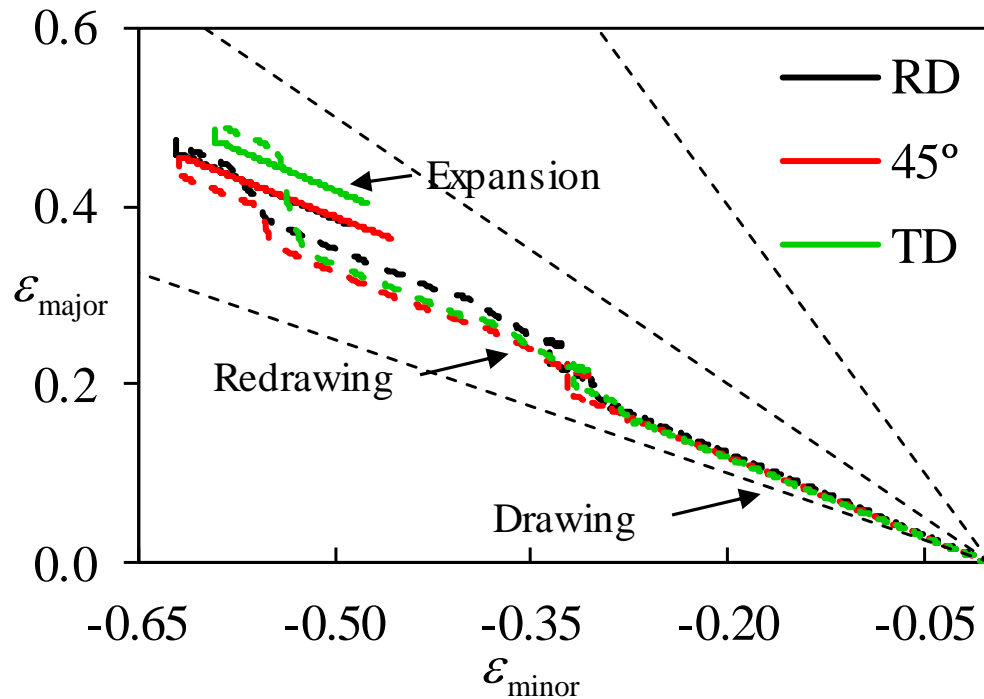


Distribution of the thickness strain at the end of the expansion phase, for the same punch displacement, for the AA5352 aluminium alloy (left) and cups after expansion (right).

# Failure Prediction after Cup Drawing, Reverse Redrawing and Expansion

## Strain paths

- Globally, the points follow a more dissimilar trend for the AA5352, highlighting the fact that this material presents a more anisotropic behaviour than the TH330 steel.
- For the AA5352 higher major strains are attained, particularly at the end of the reverse redrawing operation, which can be related with the ironing stage.



Evolution of the principal in-plane strains at the leading edge of the cup at RD, 45° with RD and TD for the TH330 steel (left) and the AA5352 aluminium alloy.

# Conclusions

- Globally, the cup height at the end of the reverse redrawing operations is well predicted.
- Nonetheless, the thickness distribution along the cup circumferential direction is underestimated, for both materials.
- For the AA5352 aluminium alloy this can be related with the occurrence of ironing of the wall in the numerical simulation, since the gap between the die and the punch of the redrawing stage does not allow to accommodate the thickening that occurs in the flange. Thus, the discrepancy can be associated with different process conditions.
- However, the result indicate that the plastic flow is not accurately described by the normal to the yield surface. The analysis of the strain history highlights the importance of the stress states located between uniaxial compression and pure shear. Unfortunately, this region of the yield surface is not covered by the set of experimental mechanical tests performed to characterize the mechanical behaviour of the material.



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